# THE ARION UNSTRUCTURED GRIDS CFD SOLVER: THEORETICAL AND USER'S MANUAL <br> Version 2.2 (Build 700-1049-gd14283f) ISCFDC Report 2023-06 



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## Abstract

This manual describes the algorithms, methods, and input and output files of the Arion code. In addition, the manual serves as the user's manual of the code. The current version of the code is the first release production version of the code, still undergoing continuous development efforts. As of the current revision, the code provides the capability to simulate inviscid, laminar, and turbulent steady flows. Currently, the flow solver contains the HLLC approximate Riemann solver, the $\mathrm{AUSM}^{+}$-up, or the AUSM-DV schemes for the approximation of the convective fluxes and the $\mathrm{k}-\omega$ TNT turbulence model. The code is fully parallel using a distributed architecture, as well as by shared memory (OpenMP) using hybrid architecture.

## Chapter 1

## Introduction

This manual describes the algorithms, methods, and input/output files of the Arion code. In addition, the manual serves as the user's manual of the code.

### 1.1 Current Release

The current version of the code has gone through various changes. As of the current revision, the code provides the capability to simulate inviscid, laminar, and turbulent steady flows. Currently, the flow solver contains the HLLC approximate Riemann solver, the AUSM ${ }^{+}$-up scheme, or the AUSM-DV schemes for the approximation of the convective fluxes. Turbulence may be modeled using either the $\mathrm{k}-\omega-\mathrm{TNT}$ or the $\mathrm{k}-\omega$ SST turbulence models. The code is fully parallel using a distributed architecture. Domain decomposition is carried out using the Metis open source library.

### 1.2 Users's Manual Arrangement

The report is arranged in the following manner: Chapter 2 contains a description of the available physical models while Chapter 3 describes the turbulence models that are used in the code. Chapter 4 is dedicated to a detailed description of the computational methods. Chapter 5 briefly describes the boundary conditions while Chapter 6 describes the type and format of unstructured meshes that the code sup-
ports. Chapter 7 describes the parallelization of the code. Chapter 8 contains a detailed description of the input file syntax, and actually serves as the code's reference manual.

## Chapter 2

## Physical Models

### 2.1 Introduction

Computer simulations are generally based upon the numerical solution of the model equations in a discretized mode. The accuracy of the computations depends mainly on the physical modeling, the numerical algorithm, and the quality of the computational mesh. At its current developmental stage, the Arion code provides the capability to simulate only single-component perfect gas flows, in particular, air flows. This chapter contains a description of the physical models that are available in the solver.

### 2.2 Single-component Perfect Gas (SPG)

### 2.2.1 Governing Equations

The equations governing single-component, perfect gas fluid flow are derived from the laws of conservation of mass, momentum, and total energy. The set of five partial differential equations is known as the Navier-Stokes equations and can be represented in a conservation-law form that is convenient for numerical simulations, namely

$$
\begin{equation*}
\frac{\partial Q}{\partial t}+\frac{\partial\left(E_{c}-E_{d}\right)}{\partial x}+\frac{\partial\left(F_{c}-F_{d}\right)}{\partial y}+\frac{\partial\left(G_{c}-G_{d}\right)}{\partial z}=0 \tag{2.1}
\end{equation*}
$$

where $Q$ is the vector of conserved mass, momentum, and energy

$$
Q=\left[\begin{array}{c}
\rho  \tag{2.2}\\
\rho u \\
\rho v \\
\rho w \\
E
\end{array}\right]
$$

where the density is denoted by $\rho$, the Cartesian velocity vector components are denoted by $u, v$ and $w$, and $E$ denotes the total (internal and kinetic) energy of the gas. The inviscid flux vectors, $E_{c}, F_{c}$, and $G_{c}$, are

$$
E_{c}=\left[\begin{array}{c}
\rho u  \tag{2.3}\\
\rho u^{2}+p \\
\rho u v \\
\rho u w \\
u(E+p)
\end{array}\right], \quad F_{c}=\left[\begin{array}{c}
\rho v \\
\rho u v \\
\rho v^{2}+p \\
\rho v w \\
v(E+p)
\end{array}\right], \quad G_{c}=\left[\begin{array}{c}
\rho w \\
\rho u w \\
\rho v w \\
\rho w^{2}+p \\
w(E+p)
\end{array}\right]
$$

and the viscous flux vectors, $E_{d}, F_{d}$, and $G_{d}$, are

$$
E_{d}=\left[\begin{array}{c}
0  \tag{2.4}\\
\tau_{x x} \\
\tau_{y x} \\
\tau_{z x} \\
\beta_{x}
\end{array}\right], \quad F_{d}=\left[\begin{array}{c}
0 \\
\tau_{x y} \\
\tau_{y y} \\
\tau_{z y} \\
\beta_{y}
\end{array}\right], \quad G_{d}=\left[\begin{array}{c}
0 \\
\tau_{x z} \\
\tau_{y z} \\
\tau_{z z} \\
\beta_{z}
\end{array}\right]
$$

where

$$
\begin{align*}
& \tau_{x x}=\lambda\left(\frac{\partial u}{\partial x}+\frac{\partial v}{\partial y}+\frac{\partial w}{\partial z}\right)+2 \mu \frac{\partial u}{\partial x} \\
& \tau_{y y}=\lambda\left(\frac{\partial u}{\partial x}+\frac{\partial v}{\partial y}+\frac{\partial w}{\partial z}\right)+2 \mu \frac{\partial v}{\partial y} \\
& \tau_{z z}=\lambda\left(\frac{\partial u}{\partial x}+\frac{\partial v}{\partial y}+\frac{\partial w}{\partial z}\right)+2 \mu \frac{\partial w}{\partial z} \\
& \tau_{x y}=\tau_{y x}=\mu\left(\frac{\partial u}{\partial y}+\frac{\partial v}{\partial x}\right) \\
& \tau_{x z}=\tau_{z x}=\mu\left(\frac{\partial u}{\partial z}+\frac{\partial w}{\partial x}\right)  \tag{2.5}\\
& \tau_{y z}=\tau_{z y}=\mu\left(\frac{\partial v}{\partial z}+\frac{\partial w}{\partial y}\right) \\
& \beta_{x}=u \tau_{x x}+v \tau_{x y}+w \tau_{x z}+\kappa \frac{\partial T}{\partial x} \\
& \beta_{y}=u \tau_{y x}+v \tau_{y y}+w \tau_{y z}+\kappa \frac{\partial T}{\partial y} \\
& \beta_{z}=u \tau_{z x}+v \tau_{z y}+w \tau_{z z}+\kappa \frac{\partial T}{\partial z}
\end{align*}
$$

where $T$ is the temperature. Stokes hypothesis, $\lambda=-\frac{2}{3} \mu$, is typically used to further simplify Equation (2.5).

Finally, in the perfect-gas model, the source-term vector, $S$, may only contain contributions from the turbulence model (see Chapter 3).

### 2.2.2 Integral Form For Moving Grids

For a three-dimensional flow through a finite volume $\Omega$, enclosed by the boundary surface $\partial \Omega \equiv S$ that is moving with a grid velocity $\bar{V}_{g}$, the integral form of the conservation equations in an inertial frame of reference is given as:

$$
\begin{equation*}
\frac{\partial}{\partial t} \int_{\Omega} Q d \Omega+\oint_{S} d \bar{S} \cdot \bar{H}=0 \tag{2.6}
\end{equation*}
$$

where

$$
\begin{equation*}
\bar{H}=\left(E_{c}-E_{d}\right) \hat{i}+\left(F_{c}-F_{d}\right) \hat{j}+\left(G_{c}-G_{d}\right) \hat{k} \tag{2.7}
\end{equation*}
$$

In Equation (2.6) the vector of dependent variables, $Q$, remains as in Equation (2.2).Similarly, the viscous flux vectors, $E_{d}, F_{d}$, and $G_{d}$, appearing in Equation (2.7), remain as in Equations (2.4) and (2.5) (see Section 2.2.1). In contrast, the inviscid flux vectors
take a form that reflects the motion of the grid as follows:

$$
\begin{align*}
& E_{c}=\left[\begin{array}{c}
\rho\left(u-u_{g}\right) \\
\rho u\left(u-u_{g}\right)+p \\
\rho v\left(u-u_{g}\right) \\
\rho w\left(u-u_{g}\right) \\
(E+p)\left(u-u_{g}\right)+u_{g} p
\end{array}\right] \\
& F_{c}=\left[\begin{array}{c}
\rho\left(v-v_{g}\right) \\
\rho u\left(v-v_{g}\right) \\
\rho v\left(v-v_{g}\right)+p \\
\rho w\left(v-v_{g}\right) \\
(E+p)\left(v-v_{g}\right)+v_{g} p
\end{array}\right] \\
& G_{c}=\left[\begin{array}{c}
\rho\left(w-w_{g}\right) \\
\rho u\left(w-w_{g}\right) \\
\rho v\left(w-w_{g}\right) \\
\rho w\left(w-w_{g}\right)+p \\
(E+p)\left(w-w_{g}\right)+w_{g} p
\end{array}\right] \tag{2.8}
\end{align*}
$$

where $u_{g}, v_{g}$, and $w_{g}$ are the Cartesian components of the grid velocity vector $\bar{V}_{g}$. Note that currently the grid velocity vector is set to $\bar{V}_{g} \equiv 0$.

### 2.2.3 Equation of State

To close the system of fluid dynamics equations, it is necessary to establish relations between the thermodynamics variables, $p, \rho, T$, and the internal energy, $e_{I}$. Assuming a perfect gas, the pressure and temperature may be obtained from the following equation of state:

$$
\begin{equation*}
p=\rho R T \tag{2.9}
\end{equation*}
$$

where $R$ is the gas constant ( $R=287.0$ for air). By assuming further that the gas is a calorically perfect gas (and hence the specific heats $C_{p}$ and $C_{v}$ are constant), the
equation of state takes the form:

$$
\begin{equation*}
p=\rho(\gamma-1) e_{I} \tag{2.10}
\end{equation*}
$$

where $e_{I}$ is the internal energy of the gas, and $\gamma$ is the (constant) ratio of specific heats $\left(c_{p} / c_{v}\right)$. In terms of the flow variables, the pressure and temperature are calculated using:

$$
\begin{align*}
p & =(\gamma-1)\left[E-\frac{1}{2} \rho\left(u^{2}+v^{2}+w^{2}\right)\right] \\
T & =\frac{\gamma-1}{R}\left[e-\frac{1}{2}\left(u^{2}+v^{2}+w^{2}\right)\right] \tag{2.11}
\end{align*}
$$

where $e=\frac{E}{\rho}$ is the specific total energy.

### 2.2.4 Transport Properties

In addition to the equation of state, it is also necessary to establish constitutive relations, namely, relations for the coefficient of viscosity, $\mu$, and the coefficient of thermal conductivity, $\kappa$. In the single-component perfect gas (SPG) model, the Sutherland formulae are exclusively used to evaluate these coefficients. The Arion code provides two different ways to evaluate $\mu$ and $\kappa$.

The first (called "molecular.sutherland.air.1", see Table 8.29) is based on the following relations:

$$
\begin{align*}
\mu & =C_{\mu_{1}} \frac{T^{\frac{3}{2}}}{T+C_{\mu_{2}}} \\
\kappa & =C_{\kappa_{1}} \frac{T^{\frac{3}{2}}}{T+C_{\kappa_{2}}} \tag{2.12}
\end{align*}
$$

The default of the coefficients $C_{\mu_{1}}, C_{\mu_{2}}, C_{\kappa_{1}}$, and $C_{\kappa_{2}}$ correspond to air and are given in Table 2.1. For the purpose of simulating a gas whose transport properties are different than air, the coefficients can be set by the user using the directives as described in Tables 8.30, 8.31, 8.32, 8.33.

| Fluid type | $C_{\mu_{1}}$ | $C_{\mu_{2}}$ | $C_{\kappa_{1}}$ | $C_{\kappa_{2}}$ |
| :---: | :---: | :---: | :---: | :---: |
| Air | $1.458 \times 10^{-6}$ | 110.4 | $2.495 \times 10^{-3}$ | 194 |

Table 2.1: Default coefficients for Sutherland formulae (type 1)

The second way to evaluate $\mu$ and $\kappa$ (called "molecular.sutherland.air.2", see Table 8.29) is based on the following relations:

$$
\begin{align*}
\mu & =\eta_{0} \frac{T_{0}-C_{0}}{T-C_{0}}\left(\frac{T}{T_{0}}\right)^{\frac{3}{2}} \\
\kappa & =\frac{c_{p} \mu}{P r} \tag{2.13}
\end{align*}
$$

where $P_{r}$ is the Prandtl number. The default of the coefficients $\eta_{0}, T_{0}$, and $C_{0}$ correspond to air and are given in Table 2.2. The coefficients can be set by the user using the directives as described in Tables 8.34, 8.35, 8.36, and 8.37.

| Fluid type | $\eta_{0}$ | $C_{0}$ | $T_{0}$ | $P_{r}$ |
| :---: | :---: | :---: | :---: | :---: |
| Air | $1.827 \times 10^{-5}$ | 120 | 291.15 | 0.72 |

Table 2.2: Default coefficients for Sutherland formulae (type 2)

### 2.3 Gas Selection

As mentioned above, the Arion code provides the means to simulate the flow of any perfect gas. This is facilitated via a series of directives that allow to set the specific gas constant, ( $R$, see Table 8.25), the the heat capacity ratio, ( $\gamma$, see Table 8.26, and the Sutherland formulae coefficients as described in Section 2.2.4.

## Chapter 3

## Turbulence Models

The unsteady Navier-Stokes equations are generally considered to govern turbulent flows in the continuum flow regime. However, turbulent flow cannot be numerically simulated as easily as laminar flow. To resolve a turbulent flow by direct numerical simulation (DNS) requires that all relevant length scales be properly resolved. Such requirements place great demands on the computer resources, a fact that renders the possibility of conducting DNS analysis about complete aircraft configurations infeasible.

A practical approach to simulating turbulent flows is to solve the time-averaged Navier-Stokes equations. These equations are know as the "Reynolds averaged NavierStokes" (RANS) equations. The averaging of the equations of motion gives rise to new terms that are called the Reynolds stresses. To solve the averaged equations, the Reynolds stress tensor must be related to the flow variables through turbulence models. The models are used to "close" the system through an additional set of assumptions. The models are classified based on the number of additional partial differential equations that must be solved. The Arion code currently contains only one turbulence model, a two-equation model.

### 3.1 RANS Turbulence Model Equations

The Arion code treats the mean flow and turbulence models equations in a unified manner. To this end, the Navier-Stokes equation set is extended to include the turbulence model equations. Consequently, the discretization of the various fluxes can be conducted in the same manner.

The equations governing turbulent flows are obtained by Favre-averaging the Navier-Stokes equations and by modeling the Reynolds stress tensor. The unknown averaged Reynolds stress tensor is modeled either using the Boussinesq assumption via a linear eddy-viscosity model or by directly solving a transport equation for each of the Reynolds stress components via a second moment closure. The general form of the resulting Navier-Stokes equations and the turbulence model equations has the form (for simplicity of the representation, with no loss of generality, the formulation under the perfect gas physical model assumption is brought herein; it can be easily extended to any physical model):

$$
\begin{equation*}
\frac{\partial Q}{\partial t}+\frac{\partial\left(E_{c}-E_{d}\right)}{\partial x}+\frac{\partial\left(F_{c}-F_{d}\right)}{\partial y}+\frac{\partial\left(G_{c}-G_{d}\right)}{\partial z}=S \tag{3.1}
\end{equation*}
$$

where $S$ is the source term associated with the turbulence model only (once again, under the perfect gas physical model assumption). Hence, for turbulent flow simulations, Equation (3.1) replaces Equation (2.1).

In what follows, the symbol $\left(^{-}\right)$indicates non-weighted averaging, the symbol ( ${ }^{\sim}$ ) signifies mass weighted Favre averaging, and the symbol ( ${ }^{\prime \prime}$ ) denotes Favre fluctuations. Depending on whether the turbulence model has one, two, or $m$ equations, the vector of dependent variables, $Q$, and the vector of source terms $S$ now take the
form:

$$
Q=\left[\begin{array}{c}
\bar{\rho}  \tag{3.2}\\
\bar{\rho} \tilde{u} \\
\bar{\rho} \tilde{v} \\
\bar{\rho} \tilde{w} \\
\tilde{E} \\
\bar{\rho} q_{1} \\
\cdots \\
\bar{\rho} q_{m}
\end{array}\right], \quad S=\left[\begin{array}{c}
0 \\
0 \\
0 \\
0 \\
0 \\
s 1 \\
\cdots \\
s_{m}
\end{array}\right]
$$

where $q$ is the vector of turbulence model dependent variables and $s$, is the source terms vector. Note that the source terms differ from model to model. The vectors $E_{c}, F_{c}$, and $G_{c}$ usually take the form:

$$
E_{c}=\left[\begin{array}{c}
\bar{\rho} \tilde{u}  \tag{3.3}\\
\bar{\rho} \tilde{u}^{2}+\bar{p} \\
\bar{\rho} \tilde{u} \tilde{v} \\
\bar{\rho} \tilde{u} \tilde{w} \\
\tilde{u}(\tilde{E}+\bar{p}) \\
\bar{\rho} \tilde{u} q_{1} \\
\cdots \\
\bar{\rho} \tilde{u} q_{m}
\end{array}\right], F_{c}=\left[\begin{array}{c}
\bar{\rho} \tilde{v} \\
\bar{\rho} \tilde{u} \tilde{v} \\
\bar{\rho} \tilde{v}^{2}+\bar{p} \\
\bar{\rho} \tilde{v} \tilde{w} \\
\tilde{v}(\tilde{E}+\bar{p}) \\
\bar{\rho} \tilde{v} q_{1} \\
\cdots \\
\bar{\rho} \tilde{v} q_{m}
\end{array}\right], G_{c}=\left[\begin{array}{c}
\bar{\rho} \tilde{w} \\
\bar{\rho} \tilde{u} \tilde{w} \\
\bar{\rho} \tilde{v} \\
\bar{\rho} \tilde{w}^{2}+\bar{p} \\
\tilde{w}(\tilde{E}+\bar{p}) \\
\bar{\rho} \tilde{w} q_{1} \\
\cdots \\
\bar{\rho} \tilde{w} q_{m}
\end{array}\right]
$$

Similarly, the vectors, $E_{d}, F_{d}$, and $G_{d}$, usually take the form:

$$
E_{d}=\left[\begin{array}{c}
0  \tag{3.4}\\
\bar{\tau}_{x x}-\overline{\rho u^{\prime \prime} u^{\prime \prime}} \\
\bar{\tau}_{y x}-\overline{\rho v^{\prime \prime} u^{\prime \prime}} \\
\bar{\tau}_{z x}-\overline{\rho w^{\prime \prime} u^{\prime \prime}} \\
\bar{\beta}_{x} \\
e_{d_{1}} \\
\cdots \\
e_{d_{m}}
\end{array}\right], \quad F_{d}=\left[\begin{array}{c}
0 \\
\bar{\tau}_{x y}-\overline{\rho u^{\prime \prime} v^{\prime \prime}} \\
\bar{\tau}_{y y}-\overline{\rho v^{\prime \prime} v^{\prime \prime}} \\
\bar{\tau}_{z y}-\overline{\rho w^{\prime \prime} v^{\prime \prime}} \\
\bar{\beta}_{y} \\
f_{d_{1}} \\
\cdots \\
f_{d_{m}}
\end{array}\right], \quad G_{d}=\left[\begin{array}{c}
0 \\
\bar{\tau}_{x z}-\overline{\rho u^{\prime \prime} w^{\prime \prime}} \\
\bar{\tau}_{y z}-\overline{\rho v^{\prime \prime} w^{\prime \prime}} \\
\bar{\tau}_{z z}-\overline{\rho w^{\prime \prime} w^{\prime \prime}} \\
\bar{\beta}_{z} \\
g_{d_{1}} \\
\cdots \\
g_{d_{m}}
\end{array}\right]
$$

where the vectors $e_{d}, f_{d}$, and $g_{d}$ differ from model to model and

$$
\begin{align*}
& \bar{\beta}_{x}=\tilde{u}\left(\bar{\tau}_{x x}-\overline{\rho u^{\prime \prime} u^{\prime \prime}}\right)+\tilde{v}\left(\bar{\tau}_{x y}-\overline{\rho u^{\prime \prime} v^{\prime \prime}}\right)+\tilde{w}\left(\bar{\tau}_{x z}-\overline{\rho u^{\prime \prime} w^{\prime \prime}}\right)+\left(\bar{\kappa}+\bar{\kappa}_{t}\right) \frac{\partial \bar{T}}{\partial x} \\
& \bar{\beta}_{y}=\tilde{u}\left(\bar{\tau}_{y x}-\overline{\rho v^{\prime \prime} u^{\prime \prime}}\right)+\tilde{v}\left(\bar{\tau}_{y y}-\overline{\rho v^{\prime \prime} v^{\prime \prime}}\right)+\tilde{w}\left(\bar{\tau}_{y z}-\overline{\rho v^{\prime \prime} w^{\prime \prime}}\right)+\left(\bar{\kappa}+\bar{\kappa}_{t}\right) \frac{\partial \bar{T}}{\partial y}  \tag{3.5}\\
& \bar{\beta}_{z}=\tilde{u}\left(\bar{\tau}_{z x}-\overline{\rho w^{\prime \prime} u^{\prime \prime}}\right)+\tilde{v}\left(\bar{\tau}_{z y}-\overline{\rho w^{\prime \prime} v^{\prime \prime}}\right)+\tilde{w}\left(\bar{\tau}_{z z}-\overline{\rho w^{\prime \prime} w^{\prime \prime}}\right)+\left(\bar{\kappa}+\bar{\kappa}_{t}\right) \frac{\partial \bar{T}}{\partial z}
\end{align*}
$$

The terms $\bar{\kappa}$ and $\bar{\kappa}_{t}$ are the averaged molecular and turbulent heat conductivities, respectively. The molecular heat conductivity is calculated using Sutherland's law (see Equation (2.12)) while the turbulent heat conductivity is calculated using

$$
\begin{equation*}
\bar{\kappa}_{t}=\frac{c_{p} \bar{\mu}_{t}}{P r_{t}} \tag{3.6}
\end{equation*}
$$

where $\bar{\mu}_{t}$ denotes the turbulent viscosity. The term $c_{p}$ is the specific heat capacity at constant pressure, $\operatorname{Pr}$ is the Prandtl number set to $\operatorname{Pr}=0.72$, and $P r_{t}$ is the turbulent Prandtl number set to $P r_{t}=0.9$. The average turbulent viscosity, $\bar{\mu}_{t}$ differs from model to model.

### 3.2 The k- $\omega$-TNT Turbulence Model

The TNT turbulence model has two clear advantages over other two-equation turbulence models: it uses a topology-free approach, and it is insensitive to the specific turbulence dissipation rate free-stream boundary condition. The source term of the model is given by:

$$
S=\left\{\begin{array}{c}
0  \tag{3.7}\\
0 \\
0 \\
0 \\
0 \\
P_{k}-\beta_{k} \bar{\rho} k \omega \\
\alpha_{\omega} \frac{\omega}{k} P_{k}-\beta_{\omega} \bar{\rho} \omega^{2}+\max (\mathcal{E}, 0)
\end{array}\right\}
$$

The production term is denoted by $P_{k}$ and it is based on the Boussinesq approximation while $\mathcal{E}$ is the cross diffusion term. The turbulent viscosity is defined as

$$
\begin{equation*}
\mu_{t}=\frac{\bar{\rho} k}{\omega} \tag{3.8}
\end{equation*}
$$

The remaining model constants are $\sigma_{k}=1.5, \sigma_{\omega}=2.0, \sigma_{d}=0.5, \beta_{\omega}=0.075$, $\beta_{k}=0.09, \alpha_{\omega}=\frac{\beta}{\beta^{*}}-\frac{\sigma_{\omega} \kappa^{2}}{\sqrt{\beta^{*}}}$, with $\kappa=0.41$.
A description of the boundary conditions appears in Section 3.4.

### 3.3 The $k$ - $\omega$-SST Model

There are numerous suggestions in the literature for two-equation turbulence models, many being variations of a few baseline models. As most two equation models contain one equation for the turbulence kinetic energy, $k$, one important issue is the quantity chosen to represent the length scale. While $\epsilon$ is the most obvious and popular option, it is one that causes significant problems in practice, especially in near-wall flows approaching separation. In computational aerodynamics, the most popular alternative to $\epsilon$ itself is the turbulent specific dissipation rate, $\omega$. The attraction of $\omega$-based models is rooted in the observation that it gives a superior representation of the near-wall behavior, especially in adverse pressure gradient regions. On the other hand, one serious flaw exhibited by $\omega$ based models is the extreme sensitivity to the value of $\omega$ at irrotational boundaries of shear flows and, by implication, also to the value in weak-shear regions within a complex shear flow. This, as well as other defects, have led Menter [1] to formulate a hybrid model which blends the $k$ - $\omega$ model near-wall regions with the $k$ - $\epsilon$ model in regions that are far from walls. In recent years, this model has become the most popular two-equation model in aeronautical CFD practice, especially in weakly separated flows. Again, over the years several variations and modifications to the original $k$ - $\omega$-SST model have appeared. The $k-\omega$ -SST-2003 (following the naming convention from the TMR website) has been chosen and implemented in the EZAir suite.

### 3.3.1 $k-\omega$-SST-2003 Model

The transport form of the compressible $k$ - $\omega$-SST-2003 turbulence model contains two transport equations. A transport equation for the turbulence kinetic energy, $k$, and a second transport equation for the turbulent specific dissipation rate, $\omega$. These transport equations take the following form:

$$
\begin{align*}
\frac{\partial \rho k}{\partial t}+\frac{\partial \rho u_{j} k}{\partial x_{j}} & =\frac{\partial}{\partial x_{j}}\left[\left(\mu+\sigma_{k} \mu_{t}\right) \frac{\partial k}{\partial x_{j}}\right]+P_{k}-\beta^{*} \rho \omega k  \tag{3.9}\\
\frac{\partial \rho \omega}{\partial t}+\frac{\partial \rho u_{j} \omega}{\partial x_{j}} & =\frac{\partial}{\partial x_{j}}\left[\left(\mu+\sigma_{\omega} \mu_{t}\right) \frac{\partial \omega}{\partial x_{j}}\right]+\frac{\gamma_{\omega}}{\mu_{t}} \rho P_{k}-\beta \rho \omega^{2} \\
& +2\left(1-F_{1}\right) \frac{\rho \sigma_{\omega 2}}{\omega} \frac{\partial k}{\partial x_{j}} \frac{\partial \omega}{\partial x_{j}} \tag{3.10}
\end{align*}
$$

where $t$ denotes the time and $x_{j}=[\mathrm{x}, \mathrm{y}, \mathrm{z}]$ denote the Cartesian coordinates. The fluid density is denoted by $\rho$ while the Cartesian velocity vector components are denoted by $u_{j}=[\mathrm{u}, \mathrm{v}, \mathrm{w}]$. The production term, denoted by $P_{k}$, is defined as

$$
\begin{equation*}
P_{k}=\Re_{i j} \frac{\partial u_{i}}{\partial x_{j}} \tag{3.11}
\end{equation*}
$$

where $\Re_{i j}=\overline{\rho u_{i}^{\prime \prime} u_{j}^{\prime \prime}}$ are the Reynolds stress tensor components.
The coefficient $\beta^{*}$ is a constant equal to $\beta^{*}=0.09$. The rest of the model coefficients, $\phi_{c}=\left(\sigma_{k}, \sigma_{\omega}, \gamma_{\omega}, \beta\right)$ are blended according to

$$
\begin{equation*}
\phi_{c}=F_{1} \phi_{1}+\left(1-F_{1}\right) \phi_{2} \tag{3.12}
\end{equation*}
$$

where the coefficients $\phi_{1}$ and $\phi_{2}$ are given in Table 3.1.
The $F_{1}$ function, proposed by Menter [1] himself, is given as:

$$
\begin{equation*}
F_{1}=\tanh \left(\mathfrak{Z}_{1}{ }^{4}\right) \tag{3.13}
\end{equation*}
$$

|  | $\sigma_{k}$ | $\sigma_{\omega}$ | $\gamma_{\omega}$ | $\beta$ |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |
| $\phi_{1}$ | 0.856 | 0.5 | $5 / 9$ | 0.075 |
| $\phi_{2}$ | 1.0 | 0.856 | 0.44 | 0.0828 |

Table 3.1: SST coefficients
with the argument $\mathfrak{Z}_{\perp}$ given by:

$$
\begin{equation*}
\mathfrak{Z}_{\perp}=\min \left[\max \left(\frac{\sqrt{k}}{\beta^{*} \omega d}, \frac{500 \mu}{\rho \omega d^{2}}\right), \frac{4 \sigma_{\omega 2} \rho k}{\max \left(2 \sigma_{\omega 2} \frac{\rho}{\omega} \frac{\partial k}{\partial x_{j}} \frac{\partial \omega}{\partial x_{j}}, 10^{-10}\right) d^{2}}\right] \tag{3.14}
\end{equation*}
$$

The turbulent viscosity is defined as

$$
\begin{equation*}
\mu_{t}=\frac{a_{1} \rho k}{\max \left(a_{1} \omega, S F_{2}\right)} \tag{3.15}
\end{equation*}
$$

where $S$ is:

$$
\begin{equation*}
S=\sqrt{2 S_{i j} S_{i j}} \tag{3.16}
\end{equation*}
$$

with

$$
\begin{equation*}
S_{i j}=\frac{1}{2}\left(\frac{\partial u_{i}}{\partial x_{j}}+\frac{\partial u_{j}}{\partial x_{i}}\right) \tag{3.17}
\end{equation*}
$$

and the function $F_{2}$ is defined as follow:

$$
\begin{equation*}
F_{2}=\tanh \left(\mathfrak{Z}_{2}^{2}\right) \tag{3.18}
\end{equation*}
$$

with

$$
\begin{equation*}
\mathfrak{Z}_{2}=\max \left(2 \frac{\sqrt{k}}{\beta^{*} \omega d}, \frac{500 \nu}{\omega d^{2}}\right) \tag{3.19}
\end{equation*}
$$

In the $k$ - $\omega$-SST-2003 version, the production term, $P_{k}$ is limited as follows

$$
\begin{equation*}
P_{k}=\min \left(P_{k}, 10 \beta^{*} \rho \omega k\right) \tag{3.20}
\end{equation*}
$$

A description of the boundary conditions appears in Section 3.4.

### 3.4 Boundary Conditions for the $\mathrm{k}-\omega$-TNT Turbulence model

To close the solution of any of the $\mathrm{k}-\omega$ models, the boundary conditions should be specified. The no-slip wall boundary conditions of $k$ and $\omega$, denoted by $k_{\text {wall }}$ and $\omega_{\text {wall }}$, respectively, are specified as follows:

$$
\begin{gather*}
k_{\text {wall }}=0  \tag{3.21}\\
\omega_{\text {wall }}=10 \frac{6 \nu}{\beta_{1}\left(\Delta d_{1}\right)^{2}} \tag{3.22}
\end{gather*}
$$

where $\Delta d_{1}$ denotes the distance between the center of the first cell neighboring the wall and the wall. The inflow boundary condition of $k$, denoted by $k_{\infty}$ for external flows is

$$
\begin{equation*}
k_{\infty}=\frac{3}{2}\left(T_{u} \cdot U_{\infty}\right)^{2} \tag{3.23}
\end{equation*}
$$

where $T u$ represents the turbulence intensity and $U_{\infty}$ is the magnitude of the inflow velocity. The inflow boundary condition of $\omega$, denoted as $\omega_{\infty}$ is specified as follows:

$$
\begin{equation*}
\omega_{\infty}=\frac{\bar{\rho}_{\infty} k_{\infty}}{\left(\mu_{t}\right)_{\infty}} \tag{3.24}
\end{equation*}
$$

with the recommended values of $\left(\mu_{t}\right)_{\infty}$ for external flows are as follows:

$$
\begin{equation*}
0.01<\frac{\left(\mu_{t}\right)_{\infty}}{(\mu)_{\infty}}<1.0 \tag{3.25}
\end{equation*}
$$

### 3.5 Evaluation of the Reynolds Stress Tensor

The TNT model is a linear eddy viscosity model (LEVM), and therefore the Reynolds stress tensor that is added to the mean flow equations is defined based on the Boussinesq assumption, namely:

$$
\begin{equation*}
\mathfrak{R}_{i j}=\mathfrak{R}_{i j}^{L E V M} \tag{3.26}
\end{equation*}
$$

where

$$
\begin{equation*}
\mathfrak{R}_{i j}^{L E V M}=2 \mu_{t}\left(S_{i j}-\frac{1}{3} \frac{\partial u_{k}}{\partial x_{k}} \delta_{i j}\right)-\frac{2}{3} \bar{\rho} k \delta_{i j} \tag{3.27}
\end{equation*}
$$

and

$$
\begin{equation*}
S_{i j}=\frac{1}{2}\left(\frac{\partial u_{i}}{\partial x_{j}}+\frac{\partial u_{j}}{\partial x_{i}}\right) \tag{3.28}
\end{equation*}
$$

Note that the turbulence kinetic energy $k$ is not available with the SA-Edwards model, therefore the term $\frac{2}{3} \bar{\rho} k \delta_{i j}$ is neglected when using the SA-Edwards model.

### 3.6 Turbulence-Mean-flow Coupling

In eddy-viscosity-based models, the coefficients of viscosity $\mu$ and thermal conductivity $\kappa$ are replaced by the relations

$$
\begin{align*}
\mu & =\bar{\mu}_{l}+\bar{\mu}_{t} \\
\kappa & =\bar{\kappa}_{l}+\frac{C_{p} \bar{\mu}_{t}}{P r_{t}} \tag{3.29}
\end{align*}
$$

to account for the effects of turbulence on the mean-flow. The turbulent Prandtl number is assumed constant $\left(\operatorname{Pr}_{t}=0.9\right)$.

## Chapter 4

## Computational Methods

### 4.1 Spatial Discretization

A conservative cell-centered finite volume methodology is employed to discretize the governing equations. The computational domain is a unstructured hybrid grid that is discretized into $N_{c v}$ non-overlapping control volumes. A control volume, $C_{v}$ is defined by a grid volume element and $\partial \Gamma$ is the volume control surface, with $\mathbf{n}=\left[n_{x}, n_{y}, n_{z}\right]^{T}$ being the outward-pointing, unit normal vector to $\partial \Gamma$. Therefore, Equation (2.6) for a control volume $C_{v}$ can be expressed as:

$$
\begin{equation*}
\frac{\partial}{\partial t} \int_{C_{v}} Q d V+\int_{\partial \Gamma} H d S=0 \tag{4.1}
\end{equation*}
$$

where $H$ is the rotated flux, namely,

$$
\begin{align*}
H & =H_{c}+H_{d} \\
H_{c} & =E_{c} n_{x}+F_{c} n_{y}+G_{c} n_{z} \\
H_{d} & =E_{d} n_{x}+F_{d} n_{y}+G_{d} n_{z} \tag{4.2}
\end{align*}
$$

The term $H_{c}$ is the convective part of the flux while $H_{d}$ is the diffusive part of the flux. The semi-discrete form of Equation(4.1) for a non-deforming cell $i$ is given by:

$$
\begin{equation*}
V_{i} \frac{d Q_{i}}{d t}=-\sum_{j \in N(i)} H_{i j} S_{i j}=R_{i} \tag{4.3}
\end{equation*}
$$

where $V_{i}$ denotes the cell volume, $Q_{i}$ is the vector of cell-averaged conservative dependent variables, $N(i)$ denotes the set of cell $i$ neighbors, $H_{i j}$ is the rotated flux vector normal to the interface $i j$ shared by cell $i$ and cell $j$, and $S_{i j}$ is the interface area. The number of cell neighbors, $N(i)$, depends on the type of the cell element. For example, a tetrahedron has 4 neighbors and therefore $N(i)=4$ whereas for a hexahedron it is $N(i)=6$. The term $R_{i}$ signifies the residual of the equations. In what follows, the subscript " $i$ " is dropped for compactness of the representation.

### 4.2 Flux Approximation Schemes

In flux difference splitting, the problem of computing the cell-face fluxes for a control volume is viewed as a series of one-dimensional Riemann problems along the direction normal to the control-volume faces. Because some of the details of the exact solution, obtained at considerable cost, are lost in the cell-averaged representation of the data, the solution of the full Riemann problem is usually replaced by methods referred to as approximate Riemann solvers. In what follows, the currently employed HLLC scheme is described in detail.

### 4.2.1 HLLC

The concept of average-state approximations was introduced by Harten, Lax and vanLeer [2] in 1983. The Harten, Lax and van-Leer (HLL) scheme is attractive because of its robustness, conceptual simplicity, and ease of coding, but it has the serious flaw of a diffusive contact surface. This is mainly because the HLL solver reduces the exact Riemann problem to two pressure waves and therefore neglects the contact surface. Toro et al [3] discussed this limitation, and proposed a modified three wave


Figure 4.1: Wave structure of the HLLC approximate Riemann solver
solver, named HLLC, where the contact discontinuity is explicitly present. The HLLC scheme is found to have the following properties:

1. Exact preservation of isolated contact discontinuities and shear waves.
2. Positivity preserving of a scalar quantity.
3. Enforcement of the entropy condition.

The resulting scheme greatly improves contact discontinuity resolution and has been successfully used to compute compressible viscous and turbulent flows [4].

The HLLC approximate Riemann solver that is implemented in the Arion code is as proposed by Batten et al [4]. The HLLC scheme assumes two intermediate states, $\mathbf{Q}_{l}^{*}$ and $\mathbf{Q}_{r}^{*}$ within the region bounded by the left moving wave, $S_{l}$, and the right moving wave, $S_{r}$ (the subscripts " $l$ " and " $r$ " denote the left and right states of the approximate Riemann problem, respectively). The states $\mathbf{Q}_{l}^{*}$ and $\mathbf{Q}_{r}^{*}$ are split by the contact discontinuity, which moves with the velocity $S_{m}$ (see Figure 4.1).

Two wave speed estimates can be used. In the first, the wave speeds $S_{l}$ and $S_{r}$ are computed according to Einfeldt et al [5] as follows:

$$
\begin{align*}
& S_{l}=\min \left[\lambda_{\min }, \lambda_{\min }^{R o e}\right]  \tag{4.4}\\
& S_{r}=\max \left[\lambda_{\max }, \lambda_{\max }^{R o e}\right] \tag{4.5}
\end{align*}
$$

where $\lambda_{\text {min }}$ is the smallest eigenvalue and $\lambda_{\max }$ is the largest eigenvalue, evaluated at the interface. Similarly, $\lambda_{\text {min }}^{\text {Roe }}$ and $\lambda_{\text {max }}^{R o e}$ are the smallest and largest eigenvalues of Roe's average matrix [6], respectively. In the second, the wave speeds $S_{l}$ and $S_{r}$ are computed according to Davis [7] as follows:

$$
\begin{align*}
S_{l} & =\min \left[\lambda_{\min }(L), \lambda_{\min }(R)\right]  \tag{4.6}\\
S_{r} & =\max \left[\lambda_{\max }(L), \lambda_{\max }(R)\right] \tag{4.7}
\end{align*}
$$

The normal velocity to the interface, denoted by $q$, is defined as:

$$
\begin{equation*}
q=\left(u-u_{g}\right) n_{x}+\left(v-v_{g}\right) n_{y}+\left(w-w_{g}\right) n_{z} \tag{4.8}
\end{equation*}
$$

The contact discontinuity speed $S_{m}$ is evaluated according to Batten et al [4] by

$$
\begin{equation*}
S_{m}=\frac{\rho_{r} q_{r}\left(S_{r}-q_{r}\right)-\rho_{l} q_{l}\left(S_{l}-q_{l}\right)+p_{l}-p_{r}}{\rho_{r}\left(S_{r}-q_{r}\right)-\rho_{l}\left(S_{l}-q_{l}\right)} \tag{4.9}
\end{equation*}
$$

This choice of $S_{m}$ enforces the equality of the two star pressures, i.e., $p^{*}=p_{l}^{*}=p_{r}^{*}$ which is obtained from

$$
\begin{equation*}
p^{*}=\rho_{l}\left(q_{l}-S_{l}\right)\left(q_{l}-S_{m}\right)+p_{l}=\rho_{r}\left(q_{r}-S_{r}\right)\left(q_{r}-S_{m}\right)+p_{r} \tag{4.10}
\end{equation*}
$$

Introducing the intermediate left state vector

$$
\mathbf{Q}_{l}^{*}=\left\{\begin{array}{c}
\rho_{l}^{*}  \tag{4.11}\\
(\rho u)_{l}^{*} \\
(\rho v)_{l}^{*} \\
(\rho w)_{l}^{*} \\
E_{l}^{*}
\end{array}\right\}=\Omega_{l}\left\{\begin{array}{c}
\rho_{l}\left(S_{l}-q_{l}\right) \\
\left(S_{l}-q_{l}\right)(\rho u)_{l}+\left(p^{*}-p_{l}\right) n_{x} \\
\left(S_{l}-q_{l}\right)(\rho v)_{l}+\left(p^{*}-p_{l}\right) n_{y} \\
\left(S_{l}-q_{l}\right)(\rho w)_{l}+\left(p^{*}-p_{l}\right) n_{z} \\
\left(S_{l}-q_{l}\right) E_{l}-p_{l} q_{l}+p^{*} S_{m}
\end{array}\right\}
$$

where $\Omega_{l} \equiv\left(S_{l}-S_{m}\right)^{-1}$. The left state flux vector becomes

$$
\mathbf{H}_{c_{l}}^{*} \equiv \mathbf{H}_{c}\left(\mathbf{Q}_{l}^{*}\right)=\mathbf{Q}_{l}^{*} S_{m}+\left\{\begin{array}{c}
0  \tag{4.12}\\
p^{*} n_{x} \\
p^{*} n_{y} \\
p^{*} n_{z} \\
p^{*} S_{m}
\end{array}\right\}
$$

and the corresponding intermediate right state vector and right flux vector are obtained from Equations (4.11), (4.12) by interchanging the subscripts $l \rightarrow r$. Finally, the numerical HLLC flux is defined as follow

$$
\mathbf{H}_{c}\left(\mathbf{Q}_{l}, \mathbf{Q}_{r}\right)=\left\{\begin{array}{ll}
\mathbf{H}_{c}\left(\mathbf{Q}_{l}\right) & \text { if } S_{l}>0  \tag{4.13}\\
\mathbf{H}_{c}\left(\mathbf{Q}_{l}^{*}\right) & \text { if } S_{l} \leq 0<S_{m} \\
\mathbf{H}_{c}\left(\mathbf{Q}_{r}^{*}\right) & \text { if } S_{m} \leq 0 \leq S_{r} \\
\mathbf{H}_{c}\left(\mathbf{Q}_{r}\right) & \text { if } S_{r}<0
\end{array}\right\}
$$

where $\mathbf{H}_{c}\left(\mathbf{Q}_{l}\right)$ and $\mathbf{H}_{c}\left(\mathbf{Q}_{r}\right)$ are the left and right analytic flux vectors, respectively.

### 4.2.2 AUSM

The advection upstream splitting method (AUSM) was first introduced in the year 1993 by Liou and Steffen [8]. The development of the AUSM was motivated by the desire to combine the efficiency of flux vector splitting methods (FVS) and the accuracy of flux differencing splitting methods (FDS). The key idea behind AUSM schemes is the the fact that the inviscid flux vector consists of two physically distinct parts, namely the convective terms and the pressure terms. The convective terms can therefore be considered as passive scalar quantities convected by a suitably defined velocity. On the other hand, the pressure flux terms are governed by the acoustics wave speeds.

### 4.2.2.1 $\mathrm{AUSM}^{+}$-up

Although AUSM schemes enjoy a demonstrated improvement in accuracy, efficiency, and robustness over existing schemes, they have been found to have deficiencies in some cases. In the year 1996, Liou improved the original AUSM, termed now the $\mathrm{AUSM}^{+}$[9]. Among the improvement features of the original AUSM scheme are the following properties: (1) exact resolution of a one-dimensional contact discontinuity and shock discontinuities, (2) positivity preserving of scalar quantities, (3) free of "carbuncle phenomenon".

In the year 2006, Liou introduced a sequel scheme to the $\mathrm{AUSM}^{+}$called the $\mathrm{AUSM}^{+}$-up [10] extended for all speed flows. The $\mathrm{AUSM}^{+}$-up is implemented in the Arion code and it is given as follows:

$$
\mathbf{F}_{c}\left(\mathbf{Q}_{l}, \mathbf{Q}_{r}\right)=\mathbf{p}_{1 / 2}+\dot{m}_{1 / 2}\left\{\begin{array}{cc}
\boldsymbol{\psi}_{l} & \text { if } M_{1 / 2}>0  \tag{4.14}\\
\boldsymbol{\psi}_{r} & \text { otherwise }
\end{array}\right\}
$$

where

$$
\boldsymbol{\psi}_{l / r}=\left\{\begin{array}{c}
1  \tag{4.15}\\
u_{l / r} \\
v_{l / r} \\
w_{l / r} \\
H_{l / r}
\end{array}\right\}
$$

the mass flux, $\dot{m}_{1 / 2}$ is defined as

$$
\dot{m}_{1 / 2}=a_{1 / 2} M_{1 / 2}\left\{\begin{array}{cc}
\rho_{l} & \text { if } M_{1 / 2}>0  \tag{4.16}\\
\rho_{r} & \text { otherwise }
\end{array}\right\}
$$

and the pressure flux, $\mathbf{p}_{1 / 2}$ is given as

$$
\mathbf{p}_{1 / 2}=\left\{\begin{array}{c}
0  \tag{4.17}\\
p_{1 / 2} n_{x} \\
p_{1 / 2} n_{y} \\
p_{1 / 2} n_{z} \\
0
\end{array}\right\}
$$

where

$$
\begin{equation*}
p_{1 / 2}=\mathcal{P}_{(5)}^{+}\left(M_{l}\right) p_{l}+\mathcal{P}_{(5)}^{-}\left(M_{r}\right) p_{r}-K_{u} \mathcal{P}_{(5)}^{+}\left(M_{l}\right) \mathcal{P}_{(5)}^{-}\left(M_{r}\right)\left(\rho_{l}+\rho_{r}\right)\left(f_{a} a_{1 / 2}\right)\left(q_{r}-q_{l}\right) \tag{4.18}
\end{equation*}
$$

is the interface pressure. The interface-normal velocity is denoted by $q, H$ denotes the specific total enthalpy, and $K_{u}$ is a constant that equals 0.75 . The remaining functions are given below. The left/right Mach number at the interface, $M_{l / r}$, is defined as follows:

$$
\begin{equation*}
M_{l / r}=\frac{q_{l / r}}{a_{1 / 2}} \tag{4.19}
\end{equation*}
$$

where $a_{1 / 2}$ is the speed of sound at the interface and it may be calculated by a simple average of $a_{l}$ and $a_{r}$ :

$$
\begin{equation*}
a_{1 / 2}=\frac{a_{l}+a_{r}}{2} \tag{4.20}
\end{equation*}
$$

Next, the Mach number at the interface, $M_{1 / 2}$ is calculated as follows:

$$
\begin{align*}
\bar{M}^{2} & =\frac{q_{l}^{2}+q_{r}^{2}}{2 a_{1 / 2}^{2}} \\
M_{o}^{2} & =\min \left(1, \max \left(\bar{M}^{2}, M_{\infty}^{2}\right)\right) \\
f_{a}\left(M_{o}\right) & =M_{o}\left(2-M_{o}\right) \\
\rho_{1 / 2} & =\frac{\rho_{l}+\rho_{r}}{2} \\
M_{1 / 2} & =\mathcal{M}_{(4)}^{+}\left(M_{l}\right)+\mathcal{M}_{(4)}^{-}\left(M_{r}\right)-\frac{K_{p}}{f_{a}} \max \left(1-\sigma \bar{M}^{2}, 0\right) \frac{p_{r}-p_{l}}{\rho_{1 / 2} a_{1 / 2}^{2}} \tag{4.21}
\end{align*}
$$

with the constants $K_{p}=0.25$ and $\sigma=1.0$. The split Mach numbers $\mathcal{M}_{m}^{+/-}$are
polynomial functions of degree $\mathrm{m}(=1,2,4)$ of the Mach number, $M$, given as follows:

$$
\begin{align*}
\mathcal{M}_{1}^{ \pm} & =\frac{1}{2}(M \pm|M|) \\
\mathcal{M}_{2}^{ \pm} & = \pm \frac{1}{4}(M \pm 1)^{2} \\
\mathcal{M}_{(4)}^{ \pm}(M) & =\left\{\begin{array}{cc}
\mathcal{M}_{(1)}^{ \pm} & \text {if }|M|>0 \\
\mathcal{M}_{(2)}^{ \pm}\left(1 \mp 16 \beta \mathcal{M}_{(2)}^{\mp}\right) & \text { otherwise }
\end{array}\right\} \tag{4.22}
\end{align*}
$$

with the constant $\beta=1 / 8$. Finally, the pressure polynomials are given as:

$$
\mathcal{P}_{(5)}^{ \pm}(M)=\left\{\begin{array}{cc}
\frac{1}{M} \mathcal{M}_{(1)}^{ \pm} & \text {if }|M| \geq 1  \tag{4.23}\\
\mathcal{M}_{(2)}^{ \pm}\left[( \pm 2-M) \mp 16 \alpha M \mathcal{M}_{(2)}^{\mp}\right) & \text { otherwise }
\end{array}\right\}
$$

with the function $\alpha=\frac{3}{16}\left(-4+5 f_{a}^{2}\right)$.

### 4.2.3 Passive Scalar Approach

The Arion code implements the passive scalar approach [4] in spatial discretization of the various model equations (e.g., turbulence, finite-rate chemistry, etc.). The passive scalar approach enables to treat the extended governing equation set (including the model equations) in a similar manner to that presented for the Navier-Stokes equations. For example, when using any of the $k-\omega$ models with the HLLC scheme, the left and right state vectors are extended as follows:

$$
\mathbf{Q}_{l}^{*}=\left\{\begin{array}{c}
\rho_{l}^{*}  \tag{4.24}\\
(\rho u)_{l}^{*} \\
(\rho v)_{l}^{*} \\
(\rho w)_{l}^{*} \\
E_{l}^{*} \\
(\rho k)^{*} \\
(\rho \phi)^{*}
\end{array}\right\}=\Omega_{l}\left\{\begin{array}{c}
\rho_{l}\left(S_{l}-q_{l}\right) \\
\left(S_{l}-q_{l}\right)(\rho u)_{l}+\left(p^{*}-p_{l}\right) n_{x} \\
\left(S_{l}-q_{l}\right)(\rho v)_{l}+\left(p^{*}-p_{l}\right) n_{y} \\
\left(S_{l}-q_{l}\right)(\rho w)_{l}+\left(p^{*}-p_{l}\right) n_{z} \\
\left(S_{l}-q_{l}\right) E_{l}-p_{l} q_{l}+p^{*} S_{m} \\
\rho k \\
\rho \phi
\end{array}\right\}
$$

The HLLC inviscid flux is then easily evaluated using:

$$
\mathbf{H}_{c_{l}}^{*} \equiv \mathbf{H}_{c}\left(\mathbf{Q}_{l}^{*}\right)=\mathbf{Q}_{l}^{*} S_{m}+\left\{\begin{array}{c}
0  \tag{4.25}\\
p^{*} n_{x} \\
p^{*} n_{y} \\
p^{*} n_{z} \\
p^{*} S_{m} \\
0 \\
0
\end{array}\right\}
$$

### 4.2.4 High Order Flux Approximations

For a first-order-accurate approximation, the left and right state vectors are simply calculated from cell-center values left and right of the interface, respectively. To obtain a higher order flux approximation, the left and right state vectors of the convective flux are evaluated using a linear reconstruction using Green's theorem or a Taylor series expansion and least squares method. A cell-wise gradient of the primitive variables is constructed, followed by a second order Taylor series expansion, the left and right states are reconstructed. Let the vector $\boldsymbol{W}=\left(W_{m} ; m=1, \ldots 7\right)$ denote the primitive variables vector (for a general $k-\omega$ turbulence model),

$$
\begin{equation*}
\boldsymbol{W}=[\bar{\rho}, \widetilde{u}, \widetilde{v}, \widetilde{w}, \bar{p}, k, \omega] \tag{4.26}
\end{equation*}
$$

then the left and right primitive variables are reconstructed as follows:

$$
\begin{align*}
\left(W_{m}\right)_{L} & =\left(W_{m}\right)_{i}+\left(\psi_{m}\right)_{i}\left(\nabla W_{m}\right)_{i} \cdot \boldsymbol{d}_{i}^{i j}  \tag{4.27a}\\
\left(W_{m}\right)_{R} & =\left(W_{m}\right)_{j}+\left(\psi_{m}\right)_{j}\left(\nabla W_{m}\right)_{j} \cdot \boldsymbol{d}_{j}^{i j} \tag{4.27b}
\end{align*}
$$

where $\boldsymbol{d}_{i}^{i j}\left(\boldsymbol{d}_{j}^{i j}\right)$ is the distance vector from the mid-point of face $i j$ to the center of cell $i(j)$, and $\psi_{m}$ is the cell limiter that is used to suppress oscillations in the solution.

### 4.3 Diffusive Flux Vector Discretization

The diffusive flux vector normal to the interface, $\mathcal{H}_{d}$, is a function of the primitive variables vector, $\mathcal{W}$, evaluated at the mid-point of face $i j, \mathcal{W}_{i j}$, and of its derivatives. The vector $\mathcal{W}_{i j}$ is calculated by averaging of adjacent cell-center values (i.e., $\mathcal{W}_{i}$ and $\left.\mathcal{W}_{j}\right)$.

### 4.4 Time Marching Schemes

The Arion code provides various possibilities for advancing Equation (4.3) in time. This section contains a brief description of the available schemes. The schemes may be classified as follows:

1. Explicit (single and multi stage) schemes
(a) Explicit Euler
(b) Third and fourth order Runge-Kutta schemes
2. Implicit schemes
(a) Point Gauss-Seidel
3. Multi-stage implicit schemes
(a) Third fourth and fifth order Runge-Kutta implicit schemes

### 4.4.1 Explicit schemes

### 4.4.1.1 Explicit Euler Scheme

Consider the semi-discrete equation ${ }^{1}$ :

$$
\begin{equation*}
V \frac{d Q}{d t}=R \tag{4.28}
\end{equation*}
$$

[^0]A simple, first-order Euler explicit time marching scheme is given by:

$$
\begin{equation*}
\Delta Q^{n}=\frac{\Delta t}{V} R^{n} \tag{4.29}
\end{equation*}
$$

where $\Delta Q^{n}$ is the increment of the solution between time levels, namely,

$$
\begin{equation*}
\Delta Q^{n}=Q^{n+1}-Q^{n} \tag{4.30}
\end{equation*}
$$

### 4.4.1.2 Runge-Kutta Schemes

Arion provides the choice of third or fourth order Runge-Kutta schemes. Consider the semi-discrete formulation as presented in Equation (4.28), the Runge-Kutta scheme formulation is as follows:

$$
\begin{align*}
Q^{(0)} & =Q^{n} \\
Q^{(k)} & =Q^{n}+\alpha_{k} \frac{\Delta t}{V} R^{(k-1)}, \quad k=1, \ldots, K \\
Q^{n+1} & =Q^{(K)} \tag{4.31}
\end{align*}
$$

where $k$ is the Runge-Kutta sub-step number, $K=3$ for third order and $K=4$ for fourth order, and $\alpha_{k}$ are the appropriate weights.

### 4.4.2 Implicit Time Marching Formulation

The fine grid spacing required to resolve the normal viscous terms close to the body surface requires in turn very small time steps and therefore it rules out the use of explicit methods. In explicit time-marching schemes the maximum time step is proportional to the minimum grid spacing. As a result the time-step limit imposed by stability is very small. In contrast, even though the operation count per time step is high, it is more efficient to use implicit methods. The development of a non-iterative implicit algorithm for the solution of the Navier-Stokes equations requires a time linearization of the nonlinear vectors $(R)$. The linearization procedure is simple since the equations are written in conservation-law form. Applying the first order Euler implicit method and utilizing the Delta form of the equations results in the following
implicit scheme:

$$
\begin{equation*}
\left(\frac{V}{\Delta t} I-\frac{\partial R}{\partial Q}\right)^{n} \Delta Q^{n}=R^{n} \tag{4.32}
\end{equation*}
$$

where $R^{n}$ is the residual at time level $n$ as define by Equation (4.3), $I$ is the identity matrix, $\Delta t$ is the time increment between levels $n$ and $n+1$, the term $\frac{\partial R}{\partial Q}$ is the Jacobian matrix. Note that the Jacobian matrix is first order and that it may be altered to improve stability.

Applying Equation (4.32) at every grid point results in a block-hepta-diagonal matrix in three dimensions. The inversion of the matrix, or its approximation, may be conducted in various manners, resulting in a wide variety of implicit time marching schemes.

### 4.4.2.1 Point Gauss-Seidel

The exact, first order Jacobian matrix is retained only for the diagonal elements and the off diagonal Jacobian matrices are linearized based on the previous time step as follows:

$$
\begin{equation*}
\frac{\partial R}{\partial Q} \Delta Q \approx\left(\frac{\partial R}{\partial Q}\right)^{n} \Delta Q^{n} \tag{4.33}
\end{equation*}
$$

Consequently, they can be moved to the right hand side.

### 4.4.2.2 Runge-Kutta Schemes

Runge-Kutta implicit schemes combine the explicit Runge-Kutta schemes as described in Section 4.4.1.2 with the PGS scheme that is described in Section 4.4.2.1 to form a robust implicit, multi-stage time marching scheme. note that this scheme requires the matrix inversions warranted by the PGS scheme at each stage and therefore requires more computer time per iteration.

## Chapter 5

## Boundary Conditions

### 5.1 Introduction

The Arion code contains a wide variety of boundary conditions. Being an unstructured finite volume code, the notion of a ghost cell is utilized throughout. However, in certain cases the Jacobian and flux are explicitly dictated rather than calculated based on the ghost. In particular, the convection Jacobian and flux. In what follows, the subscript " $g$ " signifies a ghost cell, the subscript " $r$ " signifies a real cell where the flow is solved (a "real" cell), and the subscript " $f$ " signifies the face (prescribed) value.

### 5.2 Wall Boundary Conditions

### 5.2.1 Impermeable Wall Conditions

Let $\hat{n}$ be a unit vector normal to the face of a boundary cell, whose components are $\left(n_{x}, n_{y}, n_{z}\right)$, and let $t^{1}$ and $t^{2}$ be the two unit vectors tangent to the face of a boundary
cell, the velocity components in the ghost cell are calculated by solving the system:

$$
\left[\begin{array}{ccc}
n_{x} & n_{y} & n_{z}  \tag{5.1}\\
t_{x}^{1} & t_{y}^{1} & t_{z}^{1} \\
t_{x}^{2} & t_{y}^{2} & t_{z}^{2}
\end{array}\right]\left(\begin{array}{c}
u_{g} \\
v_{g} \\
w_{g}
\end{array}\right)=\left(\begin{array}{c}
2 \bar{V}_{f} \cdot \hat{n}-\bar{V}_{r} \cdot \hat{n} \\
\bar{V}_{r} \cdot \hat{t}^{1} \\
\bar{V}_{r} \cdot \hat{t}^{2}
\end{array}\right)
$$

The prescribed velocity vector $\bar{V}_{f}$ includes any motion of the boundary surface.

### 5.2.2 No-Slip Condition

The no-slip condition is much easier to implement:

$$
\begin{equation*}
\bar{V}_{g}=2 \bar{V}_{f}-\bar{V}_{r} \tag{5.2}
\end{equation*}
$$

### 5.2.3 Adiabatic Wall

The temperature is set using:

$$
\begin{equation*}
T_{g}=T_{r} \tag{5.3}
\end{equation*}
$$

while the pressure is set using

$$
\begin{equation*}
p_{g}=p_{r} \tag{5.4}
\end{equation*}
$$

The density is evaluated using the equation of state.

### 5.3 Far Field Conditions

### 5.3.1 Turkel Type Conditions

The characteristic relations that are due-to Turkel are utilized. For supersonic inflow, the flow quantities at the inflow boundary are set based on the current values of the corresponding boundary:

### 5.3.1.1 Turkel Inlet

$$
\begin{align*}
\rho_{g} & =\rho_{\infty}  \tag{5.5}\\
\bar{V}_{g} & =\bar{V}_{\infty}  \tag{5.6}\\
p_{g} & =\frac{\rho_{\infty}}{\rho_{r}} p_{r} \tag{5.7}
\end{align*}
$$

### 5.3.1.2 Turkel Outlet

$$
\begin{align*}
\rho_{g} & =\rho_{r}+\frac{p_{\infty}-p}{a_{\infty}^{2}}  \tag{5.8}\\
\bar{V}_{g} & =\bar{V}_{r}  \tag{5.9}\\
p_{g} & =p_{\infty} \tag{5.10}
\end{align*}
$$

### 5.3.2 Riemann Type Conditions

Let $q$ be the normal to the boundary face velocity. The Riemann invariants are calculated based on the following:

$$
\begin{align*}
R^{+} & =q_{r}-\frac{2}{\gamma-1} a_{\infty} \\
R^{-} & =q_{\infty}-\frac{2}{\gamma-1} a_{r} \tag{5.11}
\end{align*}
$$

The ghost Riemann invariants are obtained using:

$$
\begin{equation*}
R_{g}=\frac{1}{2}\left(R^{+}+R^{-}\right) \tag{5.12}
\end{equation*}
$$

### 5.3.2.1 Riemann Inlet

$$
\begin{align*}
& \rho_{g}=\frac{\rho_{\infty}}{a_{\infty}^{\frac{1}{\gamma-1}}}\{\underbrace{\left[\frac{\gamma-1}{4}\left(R^{-}-R^{+}\right)\right]^{\frac{1}{\gamma-1}}}_{a_{g}}\}^{2} \\
& p_{g}=\sqrt{a_{g}} \rho_{g} \gamma \tag{5.13}
\end{align*}
$$

### 5.3.2.2 Riemann Outlet

Let $s$ be the entropy, the relations for $\rho_{g}$ and $p_{g}$ are given by:

$$
\begin{align*}
s & =\frac{\rho^{\gamma}}{\gamma p} \\
\rho_{g} & =\left(a_{g}^{2} s\right)^{\frac{1}{\gamma-1}} \\
p_{g} & =\sqrt{a_{g}} \rho_{g} \gamma \tag{5.14}
\end{align*}
$$

### 5.3.3 Fixed (Supersonic Inlet)

$$
\begin{align*}
\bar{V}_{g} & =\bar{V}_{\infty} \\
p_{g} & =p_{\infty} \\
T_{g} & =T_{\infty} \tag{5.15}
\end{align*}
$$

### 5.3.4 Extrapolation (Supersonic Outlet)

$$
\begin{align*}
\bar{V}_{g} & =\bar{V}_{r} \\
p_{g} & =p_{r} \\
T_{g} & =T_{r} \tag{5.16}
\end{align*}
$$

### 5.3.5 Inlet

These boundary conditions use extrapolation for the pressure and set to "Fixed" the rest of the variables.

$$
\begin{align*}
(\rho, u, v, w)_{g} & =(\rho, u, v, w)_{\infty} \\
p_{g} & =p_{r} \tag{5.17}
\end{align*}
$$

### 5.3.6 Outlet

These boundary conditions use a "Fixed" value for the pressure and use extrapolation for the rest of the variables.

$$
\begin{align*}
(\rho, u, v, w)_{g} & =(\rho, u, v, w)_{r} \\
p_{g} & =p_{\infty} \tag{5.18}
\end{align*}
$$

### 5.3.7 Inout

These boundary conditions are specific to low subsonic flows. With the exception of the pressure, these boundary conditions set "Fixed" conditions for inlet and "Extrapolation" conditions for outlet. Namely,

- Inlet :

$$
\begin{align*}
(\rho, u, v, w)_{g} & =(\rho, u, v, w)_{\infty} \\
p_{g} & =p_{r} \tag{5.19}
\end{align*}
$$

- Outlet :

$$
\begin{align*}
(\rho, u, v, w)_{g} & =(\rho, u, v, w)_{r} \\
p_{g} & =p_{\infty} \tag{5.20}
\end{align*}
$$

### 5.4 Symmetry Boundary Conditions

Symmetric boundary conditions are treated exactly as an adiabatic impermeable wall.

## Chapter 6

## Computational Mesh

The Arion code is considered a hybrid code since it supports various cell element types. The code supports tetrahedra, hexahedra, prism, and pyramids. Mesh generation may be conducted by any unstructured grid generator, however, users must export the mesh using a Star-CD export or a CGNS export.

### 6.1 Star-CD Export

The Star-CD export results in three files. The first, a file containing the vertex information, having the extension ".vrt." The second, a file containing the cell elements, having the extension ".cel." And finally, a file containing the boundary elements (triangles or quads), having the extension ".bnd." The ".bnd" file contains the boundary elements as well as a name for each element. The naming is conducted by the user using the grid generation package (e.g., Pointwise). The code supports two variations of the Star-CD format, the export by Pointwise and the export by CENTAUR (only 3-D export is supported).

### 6.2 CGNS Export

The CGNS export results in a single file. The file extension of the CGNS file is ".cgns."

## Chapter 7

## Parallelization

The Arion flow solver is designed to work in a distributed memory architecture using the MPI interface. The design of the code distinguishes between managing a simulation and solving the flow field. Within the distributed MPI universe, the first rank is responsible for managing the simulation and henceforth named 'manager rank'. The rest of the ranks are responsible for the flow solution and are named 'worker ranks'. The manager rank responsibility starts with the input analysis, and continuing with reading the initial geometric problem (the grid files), splitting the computational domain into parts and sending those parts to the worker ranks. Therefore, the worker ranks know only part of the computational domain, and pass boundary data among themselves. The manager rank is responsible for the the assembly of the 'restart' files, for timing all the worker threads, and for $\log$ output. Since there is a distinction between the manager rank and the worker ranks, one must have at least two ranks running, even if they reside on a single shared memory machine.

## Chapter 8

## Input File, Run Preparation, and Execution

### 8.1 Preface

The Arion code is driven through the command line with optionally additional input files having a certain syntax. An input file may be constructed using a simple text editor. The solver is invoked by typing the MPI command (depending on the MPI version of the actual machine): "mpirun [mpi options]... arion [--f input_file] [command-line arguments]"

The input file is made of groups of directives, each group is marked by two consecutive - signs. Each group has a series of options, with each option marked with one - sign. Within the input file the sign ! means a remark until the end of the line. A brief help of all the options may be printed to the screen by using the --h option. The latest additions to the code may be printed to the screen using the --new option.

### 8.1.1 Scripting Language

The input file is a simple ASCII file with certain important rules. This chapter contains a detailed description of all the available command-line options. The syntax of each of the input options, or input file lines, follows the proceeding rules:

- The "\#" symbol means that there is a comment until the next option. One may use as many comment lines as necessary.
- Each group of directives starts with two consecutive - signs, i.e., -- followed by the group name and a series of options.
- Each option is marked with one - sign.
- An option may have no parameters, one parameter, or a few parameters.
- Parameters may be assigned values.

The proceeding description of the input options, or input file lines, makes use of the following symbols:

- The "\$" symbol signifies a string input.
- The "\#" symbol signifies a numerical input.
- The "|" symbol signifies a choice selection.
- The "..." symbol signifies an option that can be repeated.
- Input entries that are enclosed by curly brackets, $\{$ \}, are required.
- Input entries that are enclosed by square brackets, [ ], are optional.


### 8.1.2 Basic Input File: Example

Listing 8.1 contains a simple, basic input file for a simple simulation of the ideal-gas flow about a two-dimensional airfoil.

```
--equation.of.state
    -name air
    -type eos.ideal.gas
    -ref.p 101325
    -ref.T }28
--bc
    -name RIE_FREE
    -type riemann
--bc
    -name IWALL
    -type impermeable.wall
--bc
    -name XZSYM
    -type 2d
--system
    -name ideal.gas.mf.inviscid
    -type ideal.gas.mf.inviscid
    -time.step 5100 cfl.exponential }25
        -cell.gradient green.gauss.node
        -limiter mlp.2d
    -log convergence cfl residual log.residual
```

```
--solve
    -time.march implicit.rk3.R.pgs
    -convection.flux hllc.roe
    -convection.jacobian hllc.roe
    -sweeps }
    -spatial.order 2
    -iterations 2000
    -save 100
    -save.path ./save/
    -eos air
    -p 101325
    -T 288
    -Mach 0.8
    -alpha 1.25
    -beta 0
    -log convergence iter
--log
    -name convergence
    -prefix ./logs/convergence
    -per iter
    -screen
--plot
    -name naca0012
    -prefix ./plots/plot
    -interval 100
```

```
--uns
    -name naca0012-j129-uns-regular
    -prefix naca0012-j129-uns-regular/naca0012-j129-uns-regular
    -log convergence cl cd
--table
    -name P_table
    -prefix ./tables/table
    -interval 10
    -plane.bc 0 0 0 0.5 0 IWALL
```

Listing 8.1: Example of a simple Arion input file

### 8.2 Grid Files

Currently, Arion supports the Star-CD and CGNS Version 3.4 exports only. A detailed description of the files is given in Chapter 6. Starting from Version 1.31, Arion uses the Metis open source library to convert the Star-CD or CGNS export to binary format. In addition, Metis assists in decomposing the computational domain into several partitions for the purpose of efficient parallel computations. The following section describes the use of the Metis library for conversion of the files to binary format. The conversion results in a new set of files with " +32 " added to all file extensions, signifying that the integers are 32 bit wide.

The new set of files now contains 5 files. The vertex information has the extension".vrt +32 ." The cell elements file has the extension ".cel +32 ." The boundary elements file has the extension ".bnd+32." In addition, two new files are generated, one with the extension "nam+32" and the other with the extension "fac +32 ." As a result, the grid is read by the code in a fast manner.

### 8.3 Conversion

The conversion is conducted using the --star2metis or -- cgns 2 metis directive as described in Table 8.1. Note that the Metis options that are described in Tables 8.1 and 8.2 are taken directly from the Metis runtime help. For further information the user is referred to the complete Metis User's Manual.

The conversion generates a new set of files, replacing the original files that were generated by the grid generation software package (e.g., Pointwise). The actual files are not split but are reordered in a manner that prepares the files for a parallel read that is efficient in terms of domain decomposition.

## Conversion

\(\left.\begin{array}{lll}\hline \hline Syntax \& \begin{array}{l}arion\{ --star2metis <br>

[metis-options]...\end{array} \& --cgns2metis\}\$prefix \#ranks \$output\end{array}\right]\)| Description | Convert the Star-CD or CGNS files to the Arion binary format and <br> use Metis to decompose the computational domain. See Table 8.2 <br> for Metis options. | Convert Star-CD files. |
| :--- | :--- | :--- |
|  | star2metis | Convert CGNS files. |
| Parameters | \$prefix | Prefix of grid files. |
|  | \#ranks | Number of partitions. |
| \$output | Prefix of output files. |  |

Table 8.1: Conversion

Metis Options

| Metis Option | Description |
| :---: | :---: |
| -ptype $\{$ rb \| kway $\}$ | Specifiy the scheme to be used for computing the k-way partitioning: rb - Recursive bisectioning, kway - Direct k -way partitioning [default]. |
| -ctype $\{$ rm \| shem $\}$ | Specify the scheme to be used to match the vertices of the graph; rm - Random matching, shem - Sorted heavyedge matching [default]. |
| -iptype \{grow \| random | Specify the scheme to be used to compute the initial partitioning, (applies only when -ptype $=$ rb); grow - Grow a bisection using a greedy scheme [default], random Compute a bisection at random. |
| -objtype \{cut \| vol\} | Specify the objective that the partitioning routines will optimize, (applies only when -ptype = kway); cut - Minimize the edgecut [default]; vol - Minimize the total communication volume. |
| -no2hop | Specify that the coarsening will not perform any 2-hop matchings when the standard matching fails to sufficiently contract the graph. |
| -contig | Specify that the partitioning routines should try to produce (applies only when -ptype = kway) partitions that are contiguous. Note that if the input graph is not connected this option is ignored. |
| -minconn | Specify that the partitioning routines should try to minimize the (applies only when -ptype = kway) maximum degree of the subdomain graph, i.e., the graph in which each partition is a node, and edges connect subdomains with a shared interface. |

Table 8.2: Metis options

## Metis Options (continued)

| Metis Option | Description |
| :---: | :---: |
| -ufactor $\# \mathrm{x}$ (where x is an integer) | Specify the maximum allowed load imbalance among the partitions. A value of x indicates that the allowed load imbalance is $1+x / 1000$. For -ptype $=r b$, the load imbalance is measured as the ratio of the $2^{*} \max ($ left,right $) /($ left + right $)$, where left and right are the sizes of the respective partitions at each bisection. For -ptype=kway, the load imbalance is measured as the ratio of max_i(pwgts[i])/avgpwgt, where pwgts[i] is the weight of the ith partition and avgpwgt is the sum of the total vertex weights divided by the number of partitions requested. For -ptype=rb, the default value is 1 (i.e., load imbalance of 1.001) For -ptype=kway, the default value is 30 (i.e., load imbalance of 1.03). |
| -niter \#i | Specify the number of iterations for the refinement algorithms at each stage of the uncoarsening process. Default is 10 . |
| -ncuts \#c | Specify the number of different partitionings that it will compute The final partitioning is the one that achieves the best edgecut or communication volume. Default is 1. |
| -seed \#s | Select the seed of the random number generator. |

Table 8.2: Metis options (continued)

### 8.3.1 Conversion Between Different Orderings

Arion provides the capabilities to start a simulation from a certain ordering and continue the simulation with a different ordering. This is conducted using the --cnv 2 cnv directive as described in Table 8.3.

## cnv2cnv

| Syntax | arion --cnv2cnv \$cnv1 \$cnv2 \$load-prefix \$save-prefix \{\$system1name $\}$... |
| :---: | :---: |
| Description | Converts Arion solution files between different orderings; creates new restart files. |
| Parameters | \$cnv1 Ordering type to convert from. |
|  | \$cnv2 Ordering type to convert to. |
|  | \$load-prefix Prefix of input files. |
|  | \$save-prefix Prefix of output files. |
|  | \$system1-name Name of converted system. |
| Examples | arion --cnv2cnv bin arion ./newsolution/oldfiles ./newsolution/newfiles ./restart/oldfiles |

Table 8.3: Conversion between different ordering (cnv2cnv) option

### 8.4 Log Control Options

Log control options are used to set up the log outputs. For example, the options are used to set up the log file name. The log control options section starts with the $--\log$ directive, followed by a series of options that are described in the following tables. It is important to note that the number of logs (and thus generated log files) is unlimited.

## Name

| Syntax | -name $\$$ name |
| :--- | :--- |
| Description | Sets the name of the log. This name is referred to by the specific <br> -log options. It can be the predefined keywords: 'stdout', 'screen', <br> or 'display': where it will be only shown on the screen. It can also <br> be: 'stderr' where it will be only directed to the standard error <br> stream. |
| Parameters | \$name $\quad$ Log name. |
| Examples | -name convergence |

Table 8.4: Log name option

## Prefix

| Syntax | -prefix \$prefix |  |
| :--- | :--- | :--- |
| Description | The log file path and name prefix. The '‘log' suffix is added to <br> obtain the actual log file name. |  |
| Parameters | \$prefix $\quad$ Prefix. |  |
| Examples | -prefix ./logs/convergence |  |

Table 8.5: Log prefix option

## Per

| Syntax | -per Stype |
| :--- | :--- |
| Description | Sets when the log is printed based on the \$type. The possibilities <br> are: iter, produced every iteration (virtual time step); step, pro- <br> duced every step (physical time step); or pos, produced every 'pos' <br> (depending on the simulation type). |
| Parameters | Stype $\quad$ Type (iter, step, or pos). |
| Examples | -per pos |

Table 8.6: Log per option

## Stdout

| Syntax | -stdout |
| :--- | :--- |
| Description | Adds echo to the standard output as well as to the log file. One can <br> also use the -screen or -display (the outcome is exactly the same). |
| Parameters | N/A |
| Examples | -screen |

Table 8.7: Log stdout option

## Stderr

| Syntax | -stderr |
| :--- | :--- |
| Description | Adds echo to the standard error as well as to the log file. |
| Parameters | N/A |
| Examples | -stderr |

Table 8.8: Log stderr option

### 8.5 Plot Control Options

Plot control options are used to set up the plot outputs. The plot control options section starts with the --plot directive, followed by a series of options that are described in the following tables.

## Name

| Syntax | -name $\$$ name |  |
| :--- | :--- | :--- |
| Description | Sets the name of the plot. This name is referred to by the specific <br> -plot options. |  |
| Parameters | \$name $\quad$ Plot name. |  |
| Examples | -name Alpha10 |  |

Table 8.9: Plot name option

## Prefix

| Syntax | -prefix \$prefix |
| :--- | :--- |
| Description | The plot file path and name prefix. The actual file number is com- <br> posed from the prefix, and the \$name as described in Table 8.120. <br> The 'fvuns' suffix is added to the plot file name. If the computa- <br> tional domain has been decomposed, the files are split as well and <br> the number of the partition is added to the file name. |
| Parameters | \$prefix $\quad$ Prefix. |
| Examples | -prefix ./plots/ |

Table 8.10: Plot prefix option

## Interval

| Syntax | -interval \#interval |  |
| :--- | :--- | :--- |
| Description | Sets the interval (of iterations/steps) to create the plot files. |  |
| Parameters | \#interval | Plot interval. |
| Examples | -interval 100 |  |

Table 8.11: Plot interval option

## Sequential/overwrite

| Syntax | -sequential / -overwrite |
| :--- | :--- |
| Description | Include position stamp in the plot files (or overwrite, without po- <br> sition stamp, default). |
| Parameters | N/A |
| Examples | -sequential |

Table 8.12: Plot sequential/overwrite option

## FVUNS/EPPIC/CGNS

| Syntax | -fvuns / -eppic / -cgns |
| :--- | :--- |
| Description | Select the file format to use, default is:-fvuns. |
| Parameters | N/A |
| Examples | -eppic <br> -cgns |

Table 8.13: Plot fvuns/eppic/cgns option

### 8.6 Table Control Options

Table control options are used to set up the table outputs. The table control options section starts with the --table directive, followed by a series of options that are described in the following tables.

## Name

| Syntax | -name \$name |  |
| :--- | :--- | :--- |
| Description | Sets the name of the table. This name is referred to by the specific <br> -table options. |  |
| Parameters | \$name | Table name. |
| Examples | -name Alpha10 |  |

Table 8.14: Table name option

## Prefix

| Syntax | -prefix \$prefix |
| :--- | :--- |
| Description | The table file path and name prefix. The '.tbl' suffix is added to <br> obtain the actual table file name. |
| Parameters | \$prefix $\quad$ Prefix. |
| Examples | -prefix ./tables/surface-pressure |

Table 8.15: Table prefix option

## Interval

| Syntax | -interval \#interval |  |
| :--- | :--- | :--- |
| Description | Sets the interval (of iterations/steps) to create the table files. |  |
| Parameters | \#interval | Table interval. |
| Examples | -interval 100 |  |

Table 8.16: Table interval option

## Sequential/overwrite

| Syntax | -sequential/-overwrite |
| :--- | :--- |
| Description | Include position stamp in the table files (or overwrite, without po- <br> sition stamp, default). |
| Parameters | N/A |
| Examples | -sequential |

Table 8.17: Table sequential/overwrite option

## Horizontal/vertical

| Syntax | -horizontal/-vertical |
| :--- | :--- |
| Description | The table type (vertical is the default). |
| Parameters | N/A |
| Examples | -horizontal |

Table 8.18: Table horizontal/vertical option

## Ray

| Syntax | $-\mathrm{ray} \# \mathrm{x} \mathrm{\# y} \mathrm{\# z} \mathrm{\# vx} \mathrm{\# vy} \mathrm{\# vz}$ |  |
| :--- | :--- | :--- |
| Description | Create a table along a predefined ray. |  |
| Parameters | $\# \mathrm{x} \# \mathrm{y} \mathrm{\# z}$ | Ray origin. |
|  | $\# \mathrm{vx} \mathrm{\# vy} \mathrm{\# vz}$ | Ray direction. |
| Examples | -ray 000111 |  |

Table 8.19: Table ray option

## Plane.bc

| Syntax | -plane.bc \#x \#y \#z \#nx \#ny \#nz \$bc-name |  |
| :--- | :--- | :--- |
| Description | Create a table along an intersection between a plane and a bound- <br> ary surface. |  |
|  | $\# \mathrm{x} \# \mathrm{y} \# \mathrm{z}$ | Plane.bc origin. |
| Parameters | $\# \mathrm{nx} \# \mathrm{ny} \# \mathrm{nz}$ | Plane.bc direction. |
|  | \$bc-name | The boundary surface name as assigned by the <br> $--\mathrm{bc}-$ name directive (see Table 8.38). |
| Examples | -plane.bc 000111 WALL |  |

Table 8.20: Table plane.bc option

### 8.7 Parallel Options

The parallel input options section starts with the --parallel directive, followed by a series of parallel options.

## Cache

| Syntax | -cache \# |  |
| :--- | :--- | :--- |
| Description | Size of the cache memory (in bytes). |  |
| Parameters | $\#$ | Cache size. |
| Examples | -cache 1000 |  |

Table 8.21: Parallel cache option

## Rank

| Syntax | ```[{-rank #rank \| -all.ranks} {-threads | -parts | -load | -read.threads} \# ]...``` |
| :---: | :---: |
| Description | Define how many OpenMP threads will be open on each rank. |
| Parameters | \#rank Rank number. |
|  | -threads Number of threads for the current rank. |
|  | -all.ranks Means that all subsequent options hold for all the ranks. |
|  | $\begin{array}{ll}\text {-threads } & \begin{array}{l}\text { Sets the number of solver threads on a specific } \\ \text { (or all) rank. }\end{array}\end{array}$ |
|  | -read.threads Use when memory is insufficient to read all the part in parallel (a significant amount of memory is needed to read a zone part, that is deallocated at the end of the read). |
|  | -parts Number of partitions. |
|  | -load <br> Changes the load of a rank, by default all ranks have load 1. |
|  | \# Load level for the current rank. |
| Examples | -rank 1 -threads 1 |
|  | -rank 2 -threads 8 |
|  | -all.ranks -threads 48 |
|  | -rank 2 -load 4 |

Table 8.22: Parallel rank option

### 8.8 Equation of State Options

The "Equation of State" input options sections start with the --equation.of.state directive, followed by a series of equation.of.state input options. Each section is used to declare a specific fluid with its equation of state and constitutive laws (e.g.' Sutherland's law). There could be more than one section, one per fluid type. It is first assigned a name to be used by the user. The current version of Arion provides the means to solve only a single fluid and therefore only a single equation of state is concurrently supported. If nothing is set then the default ideal gas parameters of air are used.

Name

| Syntax | -name \$fluid |  |
| :--- | :--- | :--- |
| Description | Name of flow medium. |  |
| Parameters | \$fluid | Flow medium. |
| Examples | -name air |  |

Table 8.23: equation.of.state name option

## Type

| Syntax | -type Seos.type.fluid |
| :--- | :--- |
| Description | Choose the type of equation of state. Available type: eos.ideal.gas <br> (see Section 2.2.3 and Equation 2.10) |
| Parameters | Seos.type.fluid $\quad$ Type of equation of state. |
| Examples | -type eos.ideal.gas |

Table 8.24: equation.of.state type option

## R

| Syntax | $-\mathrm{R} \#$ |  |
| :--- | :--- | :--- |
| Description | Set the specific gas constant. Default is 287.22 (air). |  |
| Parameters | $\#$ | Specific gas constant. |
| Examples | -R 287.22 |  |

Table 8.25: equation.of.state $R$ option

## Gamma

| Syntax | -gamma \# |  |
| :--- | :--- | :--- |
| Description | Set the heat capacity ratio $(\gamma)$. Default is 1.4 (air). |  |
| Parameters | $\#$ | Heat capacity ratio. |
| Examples | -gamma 1.4 |  |

Table 8.26: equation.of.state gamma option

## Ref

| Syntax | -ref. $\$ \#$ |  |
| :--- | :--- | :--- |
| Description | Sets reference properties. These reference values are relevant in <br> particular for the limiters. |  |
|  | -ref.p | Reference pressure. Default is 1. |
| Parameters | -ref.T | Reference temperature. Default is 1. |
|  | -ref.length | Reference length. Default is 1. <br>  <br>  <br> Examples <br>  <br>  <br>  <br> -ref.p 101325 <br> -ref.length 0.5 |

Table 8.27: equation.of.state ref option

### 8.9 Molecular

The "Molecular" input options sections start with the --molecular directive, followed by a series of molecular input options. Each section is used to declare specific type or constants for Sutherland's law. The Sutherland formulae can be set in two ways: The fist way, called molecular.sutherland.air.1, is direct coefficients for $\mu$ and $\kappa$ (see Equation 2.12)

## Name

| Syntax | -name \$name |
| :--- | :--- |
| Description | Set the name of the molecular thermodynamic relations. |
| Parameters | \$name |

Table 8.28: Molecular name option

## Type

| Syntax | -type Stype |
| :--- | :--- |
| Description | Set the type of the molecular thermodynamic relations. <br> Available types are: molecular.sutherland.air.1 and molecu- <br> lar.sutherland.air.2 (see Section 2.2.4, Equation 2.12). |
| Parameters | Stype <br> Type of the molecular thermodynamic rela- <br> tions. |
| Examples | -type molecular.sutherland.air.1 |

Table 8.29: molecular type option

## Mu1

| Syntax | - Mu1 \#Cmu1 |
| :--- | :--- |
| Description | Sets the first coefficient for the Sutherland molecular viscosity for- <br> mula; Default is 1.458e-06 (air, see Equation 2.12 and Table 2.1). |
| Parameters | \#Cmu1 | First coefficient for the Sutherland formula 9.

Table 8.30: Molecular Mu1 option

## Mu2

| Syntax | -Mu 2 \#Cmu2 |  |
| :--- | :--- | :--- |
| Description | Sets the second coefficient for the Sutherland molecular viscosity <br> formula; Default is 110.3 (air, see Equation 2.12 and Table 2.1). |  |
| Parameters | \#Cmu2 | Second coefficient for the Sutherland formula |
| Examples | -Mu2 110.3 |  |

Table 8.31: Molecular Mu2 option

## Ka1

| Syntax | -Ka1 \#Cka1 |  |
| :--- | :--- | :--- |
| Description | Sets the first coefficient for the Sutherland thermal conductivity <br> formula; Default is 2.495e-03 (air, see Equation 2.12 and Table 2.1). |  |
| Parameters | \#Cka1 | First coefficient for the Sutherland formula |
| Examples | -Ka1 2.495e-03 |  |

Table 8.32: Molecular Ka1 option

## Ka2

| Syntax | -Ka2 \#Cka2 |  |
| :--- | :--- | :--- |
| Description | Sets the second coefficient for the Sutherland heat conductivity <br> formula; Default is 194.0 (air, see Equation 2.12 and Table 2.1). |  |
| Parameters | \#Cka2 | Second coefficient for the Sutherland formula |
| Examples | -Ka2 194.0 |  |

Table 8.33: Molecular Ka2 option

## Eta0

| Syntax | $-\mathrm{Eta0} \# \mathrm{Eta0}$ |
| :--- | :--- |
| Description | Sets $\eta_{0}$ for the Sutherland molecular viscosity formula; Default is <br> $1.827 \times 10^{-5}$ (air, see Equation 2.13 and Table 2.2). |
| Parameters | \#Eta0 $\quad$ Coefficient for the Sutherland formula |
| Examples | $-\mathrm{Eta0} 1.827 \times 10^{-5}$ |

Table 8.34: Molecular Eta0 option

## C0

| Syntax | $-\mathrm{C} 0 \# \mathrm{C} 0$ |
| :--- | :--- |
| Description | Sets $C_{0}$ for the Sutherland molecular viscosity formula; Default is <br> 120 (air, see Equation 2.13 and Table 2.2). |
| Parameters | $\# \mathrm{C} 0$ |$\quad$ Coefficient for the Sutherland formula.$~\left(\begin{array}{lll}\text { Examples } & -\mathrm{C} 0120 & \end{array}\right.$

Table 8.35: Molecular C0 option

## T0

| Syntax | -T 0 \#T0 |  |
| :--- | :--- | :--- |
| Description | Sets $T_{0}$ for the Sutherland molecular viscosity formula; Default is <br> 291.15 (air, see Equation 2.13 and Table 2.2). |  |
| Parameters | \#T0 | Coefficient for the Sutherland formula |
| Examples | -T0 291.15 |  |

Table 8.36: Molecular T0 option

## Prandtl

| Syntax | -Prandtl \#Prandtl |  |
| :--- | :--- | :--- |
| Description | Sets the Prandtl number; Default is 0.72 (air, see Equation 2.13 <br> and Table 2.2). |  |
| Parameters | \#Prandtl $\quad$ Prandtl number |  |
| Examples | -Prandtl 0.72 |  |

Table 8.37: Molecular Prandtl option

### 8.10 BC Options

Boundary conditions are set for each boundary cell, based on the name that has been assigned by the user (see Chapter 6). For each name, representing a group of boundary cells, the boundary conditions are set in two steps. First, assign the name, and second, assign the type. Each group starts with the --bc directive, followed by the name and type as follows:.

## Name

| Syntax | -name \$name |  |
| :--- | :--- | :--- |
| Description | Name of the boundary as set in Pointwise. |  |
| Parameters | \$name | Name of boundary. |
| Examples | -name WALL |  |

Table 8.38: BC name option

## Type

| Syntax | -type Stype |  |
| :--- | :--- | :--- |
| Description | Type of boundary condition. See Chapter 5 and Table 8.40 for <br> available types. |  |
| Parameters | \$type | Type of boundary condition. |
| Examples | -type noslip.wall |  |

Table 8.39: BC type option

## Boundary Condition Types

| BC type | Description (see Chapter 5 for details) |
| :--- | :--- |
| impermeable.wall | Impermeable wall. |
| noslip.wall | No slip wall. |
| automatic.wall.funct | Automatic wall function. |
| nichols.wall.function | Nichols type wall function. |
| riemann | Riemann type outer boundary conditions. |
| riemann.inlet | Riemann type inlet boundary conditions. |
| riemann.outlet | Riemann type outlet boundary conditions. |
| turkel | Turkel type outer boundary conditions. |
| turkel.inlet | Turkel type inlet boundary conditions. |
| turkel.outlet | Turkel type outlet boundary conditions. |
| inlet | Inlet type outer boundary conditions. |
| outlet | outlet type outer boundary conditions. |
| inout | Inout outer boundary conditions. |
| extrap | Zero order extrapolation. |
| fixed | Fixed boundary conditions. |
| symmetry | Symmetry type conditions. |
| $2 d$ | Two dimensional domain conditions. |

Table 8.40: Boundary condition types

## Log

| Syntax | $-\log \$ \log [\log$-options $] \ldots$ |
| :--- | :--- |
| Description | Report in log file. See Table 8.42 for log options list. |
| Parameters | $\$ \log \quad$ Log name. |
| Examples | $-\log$ coefficients cl cd |

Table 8.41: Boundary conditions log option

## BC Log Options

| Log type | Description |
| :--- | :--- |
| wet.surface | Wet surface area. |
| p.center.x | Center of pressure $x$ coordinate. |
| p.center.y | Center of pressure $x$ coordinate. |
| p.center.z | Center of pressure $x$ coordinate. |
| p.center.xFy | Center of pressure $x$ coordinate. |
| p.center.xFz | Center of pressure $x$ coordinate. |
| p.center.yFx | Pressure center sum $\left(y^{*} \mathrm{dFx}\right) / \mathrm{Fx}$ coordinate. |
| p.center.yFz | Pressure center sum $\left(\mathrm{y}^{*} \mathrm{dFz}\right) / \mathrm{Fz}$ coordinate. |
| p.center.zFx | Pressure center sum $\left(\mathrm{z}^{*} \mathrm{dFx}\right) / \mathrm{Fx}$ coordinate. |
| p.center.zFy | $X$ Pressure center sum $(\mathrm{z} * \mathrm{dFy}) /$ Fy coordinate. |
| fx | $Y$ coordinate direction force. |
| fy | $Z$ coordinate direction force. |
| fz | Force in x direction due to pressure. |
| fx.pressure |  |



| fy.pressure | Force in y direction due to pressure. |
| :--- | :--- |
| fz.pressure | Force in $z$ direction due to pressure. |
| fx.friction | Force in $x$ direction due to friction. |
| fy.friction | Force in y direction due to friction. |
| fz.friction | Force in z direction due to friction. |
| lift | Lift force. |
| drag | Drag force. |
| mx | Moment about $X$ coordinate direction. |
| my | Moment about $Y$ coordinate direction. |
| $m z$ | $Y$ coordinate direction force coefficient. |
| cfx | $Z$ coordinate direction force coefficient. |
| cfy | Moment coefficient about $X$ coordinate direction. |
| cfz | Moment coefficient about $Y$ coordinate direction. |
| cmx | Moment coefficient about $Z$ coordinate direction. |
| cmy | Lift coefficient. |
| cmz | Drag coefficient. |
| cl |  |

Table 8.42: BC log options

### 8.10.1 Wall Distance Calculations

The following directives pertain to wall type boundary conditions. Normally, one would like to calculate wall distance based on whether a specific boundary has been assigned wall conditions. However, sometimes it is required to override this default. Note that the wall distance is used only for turbulence models that require wall distance. The following two directives are exactly for that. They should be used along with a wall boundary condition.

## Wall.distance

| Syntax | -wall.distance |
| :--- | :--- |
| Description | Explicitly set wall distance search for a specific boundary. Default: <br> for all walls. |
| Parameters | N/A |
| Examples | -wall.distance |

Table 8.43: BC wall.distance option

## No.wall.distance

| Syntax | -no.wall.distance |
| :--- | :--- |
| Description | Explicitly disable wall distance search for a specific boundary. De- <br> fault: for all boundaries other than walls. |
| Parameters | N/A |
| Examples | -no.wall.distance |

Table 8.44: BC no.wall.distance option

### 8.10.2 Freestream Conditions Override

## Mach

| Syntax | - Mach \#M |  |
| :--- | :--- | :--- |
| Description | Override the freestream Mach number. |  |
| Parameters | $\# \mathrm{M}$ | Freestream Mach number. |
| Examples | - Mach 0.95 |  |

Table 8.45: BC Mach option

## Velocity.magnitude

| Syntax | -velocity.magnitude \#V |
| :--- | :--- |
| Description | Override the freestream velocity $[\mathrm{m} / \mathrm{s}]$. |
| Parameters | $\# \mathrm{~V} \quad$ Freestream velocity $[\mathrm{m} / \mathrm{s}]$. |
| Examples | -velocity.magnitude 200 |

Table 8.46: BC velocity.magnitude option

## Alpha

| Syntax | -alpha \#aoa |  |
| :--- | :--- | :--- |
| Description | Override the freestream angle of attack [degrees]. |  |
| Parameters | \#aoa | Freestream angle of attack [degrees]. |
| Examples | -alpha 5 |  |

Table 8.47: BC alpha option

## Beta

| Syntax | -beta \#beta |  |
| :--- | :--- | :--- |
| Description | Override the freestream side slip angle [degrees]. |  |
| Parameters | \#beta | Freestream side slip angle [degrees]. |
| Examples | -beta 3 |  |

Table 8.48: BC beta option

## U

| Syntax | $-\mathrm{u} \# \mathrm{u}$ |  |
| :--- | :--- | :--- |
| Description | Override the freestream $x$ coordinate direction velocity $[\mathrm{m} / \mathrm{s}]$. |  |
| Parameters | $\# \mathrm{u}$ | Freestream <br> $[\mathrm{m} / \mathrm{s}]$. |
| Examples coordinate direction velocity |  |  |

Table 8.49: BC u option

| $\mathbf{V}$ |  |  |
| :--- | :--- | :--- |
| Syntax | $-\mathrm{v} \# \mathrm{v}$ |  |
| Description | Override the freestream $y$ coordinate direction velocity $[\mathrm{m} / \mathrm{s}]$. |  |
| Parameters | $\# \mathrm{v}$ | Freestream <br> $[\mathrm{m} / \mathrm{s}]$. |
| Examples coordinate direction velocity |  |  |

Table 8.50: BC v option

## W

Syntax $\quad-$ w \#w

Description Override the freestream $z$ coordinate direction velocity $[\mathrm{m} / \mathrm{s}]$.

| Parameters $\# \mathrm{w}$ | Freestream $z$ coordinate direction velocity <br> $[\mathrm{m} / \mathrm{s}]$. |
| :--- | :--- |

Examples -w 10

Table 8.51: BC w option

| T |  |
| :---: | :---: |
| Syntax | -T \#T |
| Description | Override the freestream temperature [K]. |
| Parameters | \#T Freestream temperature [K]. |
| Examples | -T 300 |

Table 8.52: BC T option

## p

| Syntax | $-\mathrm{p} \# \mathrm{p}$ |  |
| :--- | :--- | :--- |
| Description | Override the freestream pressure [Pa]. |  |
| Parameters | $\# \mathrm{p}$ | Freestream pressure [Pa]. |
| Examples | -p 105000 |  |

Table 8.53: BC p option

## Trb.intensity

| Syntax | -trb.intensity \#ti |  |
| :--- | :--- | :--- |
| Description | Override the freestream turbulent intensity (in absolute fraction, <br> not percentage). |  |
| Parameters | \#ti | Freestream turbulent intensity (in absolute <br> fraction, not percentage). Default is 0.001. |
| Examples | -trb.intensity 0.01 |  |

Table 8.54: BC trb.intensity option

### 8.11 System Options

A system refers to a "System of Equations," e.g., Euler or Reynolds Averaged NavierStokes equations. Other examples may include, turbulence model equations or various physical model equations (not included in the current revision of the code). Each system starts with the directive --system, followed by a series of options.

Certain systems require that an additional, complimentary system would be defined. For example, when simulating turbulent flows it is required to define a mean flow system that is consistent with the turbulence model selected and a second system to solve the actual turbulence model equations.

## Type

$\left.$| Syntax | -type \$type |
| :--- | :--- |
| Description | Type of equation set to be solved. |
| Parameters | \$type | | Type of equation set. See Table 8.56 for equa- |
| :--- |
| tion system types. | \right\rvert\,

Table 8.55: System type option

## System Types

| System type | Description |
| :--- | :--- |
| ideal.gas.mf.inviscid | Solve the Euler equations assuming inviscid, ideal gas <br> flow. |
| ideal.gas.mf.viscous | Solve the Navier-Stokes equations assuming laminar <br> ideal gas flow. |
| ideal.gas.mf.tnt | Solve the Navier-Stokes equations assuming turbulent <br> ideal gas flow (using the $k-\omega$-TNT turbulence model). <br> This assumes an additional system for solving the $k-\omega$ - <br> TNT turbulence model equations. |
|  | Solve the Navier-Stokes equations assuming turbulent <br> ideal gas flow (using the $k-\omega$-SST turbulence model). <br> This assumes an additional system for solving the $k-\omega$ - <br> SST turbulence model equations. |
|  | Solve the $k-\omega$-TNT turbulence model equations. |
| turbulent.kw.tnt | Solve the $k-\omega$-SST turbulence model equations. |

Table 8.56: System types

## Cell.gradient

$\left.\begin{array}{ll}\hline \hline \text { Syntax } & \text {-cell.gradient \$method } \\ \hline \text { Description } & \begin{array}{l}\text { Method to calculate the cell center gradient that is required for } \\ \text { high order approximations. }\end{array} \\ \hline \text { Parameters } & \text { \$method }\end{array} \begin{array}{l}\text { Method for cell gradient calculation. See Ta- } \\ \text { ble 8.58 for a list of available cell gradient } \\ \text { methods. }\end{array}\right]$

Table 8.57: System cell.gradient option

## Cell Gradient Types

| Cell Gradient type | Description |
| :--- | :--- |
| green.gauss.node | Calculate cell gradient based on the Green-Gauss The- <br> orem using node reconstruction (default). |
| green.gauss.cell | Calculate cell gradient based on the Green-Gauss The- <br> orem using cell center reconstruction. |
| least.square.1 | Calculate cell gradient based on least square approxima- <br> tions using $r$ (the distance) as the weight. |
| least.square.1.5 | Calculate cell gradient based on least square approxima- <br> tions using $r^{1.5}$ as the weight. |
| least.square.2 | Calculate cell gradient based on least square approxima- <br> tions using $r^{2}$ as the weight. |

Table 8.58: Cell gradient types

## Face.gradient

| Syntax | -face.gradient \$method |
| :--- | :--- |
| Description | Method to calculate the face gradient that is required for viscous <br> fluxes calculations. |
| Parameters | \$method |
| Examples | Method for face gradient calculation. See Ta- <br> ble 8.60 for a list of available face gradient <br> methods. |

Table 8.59: System face.gradient option

## Face Gradient Types

| Face Gradient type | Description |
| :--- | :--- |
| diamond | Calculate face gradient based on the Green-Gauss The- <br> orem using a diamond-like shape (default). |
| thin.layer | Calculate face gradient based on the thin layer assump- <br> tion. |
| hasselbacher | Calculate face gradient based on defect correction by <br> Hasselbacher. |

Table 8.60: Face gradient types

## Limiter

| Syntax | -limiter \$limiter |  |
| :--- | :--- | :--- |
| Description | Type of limiter. |  |
| Parameters | $\$$ limiter | Type of limiter. See Table 8.62 for limiter <br> types. |
| Examples | -limiter venka.2d |  |

Table 8.61: Limiter option

## Limiter Types

| Limiter type | Description |
| :--- | :--- |
| none | No limiter. |
| 1st | First order. |
| venka.2d | Venkatakrishnan limiter (2D domain). |
| venka.3d | Venkatakrishnan limiter (3D domain). |
| mlp.2d | MLP-u2 limiter (2D domain). |
| mlp.3d | MLP-u2 limiter (3D domain). |

Table 8.62: Limiter types

## Venka.k

| Syntax | -venka.k \#k |  |
| :--- | :--- | :--- |
| Description | Change the Venkatakrishnan limiter coefficient. Default is 5. |  |
| Parameters | $\# \mathrm{k}$ | Venkatakrishnan limiter coefficient. |
| Examples | -venka.k 5 |  |

Table 8.63: System venka.k option

## Time.step

| Syntax | -time.step \#initial \#iterations \{cfl.linear \| cfl.exponential cfl.tangential |dt.linear \| dt.exponential | dt.tangential \} \#final |  |
| :---: | :---: | :---: |
| Description | Sets the CFL number or time step (first order single time stepping). |  |
| Parameters | \#initial | Initial CFL number or time step. |
|  | \#iterations | Number of iteration for which the CFL number or time step grows from \#initial to \#final. |
|  | cfl.linear | Linear growth of the CFL number. |
|  | cfl.exponentia | Exponential growth of the CFL number. |
|  | cfl.tangential | Hyperbolic tangent growth of the CFL number. |
|  | dt.linear | Linear growth of the time step. |
|  | dt.exponentia | Exponential growth of the time step. |
|  | dt.tangential | Hyperbolic tangent growth of the time step. |
|  | \#final | Final CFL number or time step. |
| Examples | -time.step 550 cfl.linear 10 |  |

Table 8.64: System CFL option

## Implicit.jacobi

| Syntax | -implicit.jacobi |
| :--- | :--- |
| Description | Use Jacobi instead of the default Gauss-Seidel. |
| Parameters | N/A |
| Examples | -implicit.jacobi |

Table 8.65: System implicit.jacobi option

## Convection.noslip.diagonal

| Syntax | -convection.noslip.diagonal \{normal\|analytic \|implicit.on.noslip\} |
| :--- | :--- |

Table 8.66: System convection.noslip.diagonal option

## Convection.impermeable.diagonal

| Syntax | -convection.impermeable.diagonal \{normal $\mid$ analytic $\mid$ im- <br> plicit.on.noslip\} |
| :--- | :--- |
| Description | Selects the way the diagonal convective jacobian is estimated on <br> impermeable boundaries. |
| normal $\quad$The inviscid diagonal is evaluated directly based <br> on the scheme. |  |
| Parameters | analytic $\quad$Use analytical Jacobian <br> implicit.on.noImplicit treatment of wall boundary conditions <br> through the Jacobian. <br> Examples-convection.impermeable.diagonal analytic |

Table 8.67: System convection.impermeable.diagonal option

## Convection.symmetry.diagonal

| Syntax | -convection.symmetry.diagonal \{normal <br> plicit.on.noslip\} |
| :--- | :--- |
| Description | Selects the way the diagonal convective jacobian is estimated on <br> symmetry boundaries. |
| normal $\quad$The inviscid diagonal is evaluated directly based <br> on the scheme. |  |
| Parameters | analytic <br> implicit.on.no Implicit treatment of wall boundary conditions <br> through the Jacobian. |
| Examples | -convection.symmetry.diagonal analytic |

Table 8.68: System convection.symmetry.diagonal option

## Realizability.trb.w

| Syntax | -realizability.trb.w |
| :--- | :--- |
| Description | Adds realizability condition for omega (applies only to $k-\omega$-SST <br> turbulence model). |
| Parameters | N/A |
| Examples | -realizability.trb.w |

Table 8.69: System realizability.trb.w option

## Source.mpk

| Syntax | -source.mpk \#mpk |
| :--- | :--- |
| Description | Limit turbulence model production (applies only to $k-\omega$ turbulence <br> models). |
| Parameters | $\# \mathrm{mpk}$ |$\quad$ Upper limit for production term..

Table 8.70: System source.mpk option

## Damp

| Syntax | -damp \#damp-factor |
| :--- | :--- |
| Description | Set damping to the convection Jacobian. Values that are less than <br> unity increase stability. Not recommended for turbulence model <br> equations. The recommended damping factor is 0.5-1.0. Default is <br> 1. |
| Parameters | \#damp-factor $\quad$ Damping factor. |
| Examples | -damp 0.75 |

Table 8.71: System damp option

## Relax

| Syntax | -relax \#relax-factor |
| :--- | :--- |
| Description | Set relaxation to the solution increment. The recommended relax- <br> ation factor is 0.5-1.0. Default is 1. |
| Parameters | \#relax-factor $\quad$ Relaxation factor. |
| Examples | -relax 0.75 |

Table 8.72: System relaxation option

## iteration.convergence

| Syntax | -iteration.convergence \#criterion |
| :--- | :--- |
| Description | Set the convergence criterion $(\log (\operatorname{Res} / \operatorname{Res} 0))$, default is ignored. <br> For unsteady flows this would be the convergence of the whole sim- <br> ulation. For dual time this would be convergence of the iterations. |
| Parameters | \#criterion Convergence criterion in terms of $[\log (\operatorname{Res} / \operatorname{Res} 0)]$. |
| Examples | -iteration.convergence -5 |

Table 8.73: System iteration.convergence option

## 2d.tolerance

| Syntax | -2d.tolerance \#tolerance |
| :--- | :--- |
| Description | Tolerance for two-dimensional detection. |
| Parameters | \#tolerance $\quad$ Set the tolerance. |
| Examples | -2 d.tolerance 1e-8 |

Table 8.74: System 2d.tolerance option

## Log

| Syntax | $-\log \$ \log [\log$-options] ... |
| :--- | :--- |
| Description | Report in log file. See Table 8.76 for log options list. |
| Parameters | $\$ \log \quad$ Log name. |
| Examples | $-\log$ coefficients cl cd |

Table 8.75: System log option

## System Log Options

| Log type | Description |
| :--- | :--- |
| cfl | System CFL. |
| dt | System $\Delta t$. |
| time | Time. |
| residual | System residual. |
| log.residual | System log of the residual. |
| minimal.timestep | Minimal time step. |
| orig(minimal.timestep) | Minimal time step original cell index. |
| cell(minimal.timestep) | Minimal time step zonal cell index. |
| zone(minimal.timestep) | Minimal time step zone index. |
| orig(res) | Max residual original cell number. |
| cell(res) | Max residual zonal cell number. |
| zone(res) | Max residual zone number. |
| max(mt) | Max of the turbulence viscosity (where applicable). |
| cell(mt) | Max turbulent viscosity cell number (where applicable). |
| zone(mt) | Max turbulent viscosity zone number (where applica- |

Table 8.76: System log options

## Plot

| Syntax | -plot \$plot [plot-options] |
| :---: | :---: |
| Description | Functions to include in FV-UNS file. See Table 8.78 for plot functions list. |
| Parameters | \$plot Plot name. |
| Examples | -plot NACA0012 r p velocity residual |

Table 8.77: System plot option

## Plot Functions

| Plot functions | Description |
| :---: | :---: |
| residual | Residual field. |
| relax | Relaxation field. |
| velocity | Velocity vector field (where applicable). |
| $\{\mathrm{u}\|\mathrm{v}\| \mathrm{w}\}$ | Velocity vector field components (scalars, where applicable). |
| r | Density field (where applicable). |
| p | Pressure field (where applicable). |
| Cp | Pressure coefficient (where applicable). |
| Cf | Skin-friction coefficient (where applicable). |
| T | Temperature field (where applicable). |
| \{lim.r \| lim.p | lim.u|lim.v|lim.w | Limiter fields (where applicable). |
| wall.distance | Wall distance field (where applicable). |
| mt | Turbulent viscosity field (where applicable). |
| trb.k | Turbulent kinetic energy field (where applicable). |
| trb.w | Turbulent specific dissipation rate field (where applicable). |
| \{trb.lim.k \| trb.lim.w | Turbulence model limiters (where applicable). |
| yplus | $y^{+}$(where applicable). |
| Tw | Magnitude of $\bar{\tau}_{\text {wall }}$ (where applicable). |
| Tw.vec | The vector $\bar{\tau}_{\text {wall }}$ (where applicable). |
| $\operatorname{Tw}\{\mathrm{x}\|\mathrm{y}\| \mathrm{z}\}$ | $\mathrm{X}\|\mathrm{Y}\| \mathrm{Z}$ direction component of $\bar{\tau}_{\text {wall }}$. |

### 8.12 Solve Options

The solve input options section starts with the --solve directive, followed by a series of solve options.

## Convection.flux

$\left.$| Syntax | -convection.flux \$method |
| :--- | :--- |
| Description | Set the convection flux approximation method. |
| Parameters | \$method | | Flux approximation method. See Table 8.80 |
| :--- |
| for available convection flux types. | \right\rvert\,

Table 8.79: Solve convection.flux option

## Convection Flux Types

| Convection flux type | Description |
| :--- | :--- |
| hllc.roe | HLLC Roe. |
| hllc.davis | HLLC Davis. |
| ausm | AUSM. |
| ausm.up | AUSM $^{+}$-up |
| ausm.dv | AUSM-DV |

Table 8.80: Convection flux types

## Convection.jacobian

| Syntax | -convection.jacobian \$jacobian |
| :--- | :--- |
| Description | Set the convection Jacobian. See Table 8.82 for available convection <br> Jacobian types. |
| Parameters | \$jacobian $\quad$ Jacobian. |
| Examples | -convection.jacobian hllc.roe |

Table 8.81: Solve convection.jacobian option

## Convection Jacobian Types

| Convection Jacobian type | Description |
| :--- | :--- |
| hllc.roe | HLLC Roe. |
| hllc.davis | HLLC Davis. |
| van.leer | van Leer. |
| rossow.low.mach | Low Mach number Rossow. |
| matrix.free | Matrix free. |

Table 8.82: Convection Jacobian types

## Spatial.order

| Syntax | -spatial.order \# |  |
| :--- | :--- | :--- |
| Description | Set the convection flux spatial order. Available options are either 1 <br> for first order or 2 for second order. |  |
| Parameters | $\#$ | Convection flux approximation order. |
| Examples | -spatial.order 2 |  |

Table 8.83: Solve spatial.order option

## Sweeps

| Syntax | -sweeps \# |  |
| :--- | :--- | :--- |
| Description | Set the number of sweeps within an iteration. |  |
| Parameters | $\#$ | Number of sweeps. Can be any even number. <br> Default is 6. |
| Examples | -sweeps 4 |  |

Table 8.84: Solve sweeps option

## Time.march

| Syntax | -time.march \$method |
| :--- | :--- |
| Description | Set the time marching method. See Table 8.86 for a list of available <br> time marching methods. |
| Parameters | \$method $\quad$ Time marching method. |
| Examples | -time.march implicit.pgs |

Table 8.85: Solve time.march option

## Time Marching Methods

| Time marching method | Description |
| :--- | :--- |
| explicit.euler | Explicit Euler time marching scheme. |
| explicit.rk3 | Third order Runge-Kutta explicit time marching <br> scheme. |
| explicit.rk4 | Fourth order Runge-Kutta explicit time marching <br> scheme. |
| implicit.pgs | Implicit point Gauss-Seidel time marching scheme. |
| implicit.b2.pgs | Second order implicit B2 time marching scheme. |
| implicit.heun.R.pgs | Second order Runge-Kutta implicit point Gauss-Seidel <br> time marching scheme. |
| implicit.rk3.R.pgs | Third order Runge-Kutta implicit point Gauss-Seidel <br> time marching scheme. |
| implicit.rk4.R.pgs | Fourth order Runge-Kutta implicit point Gauss-Seidel <br> time marching scheme. |
| implicit.rk5.R.pgs | Fifth order Runge-Kutta implicit point Gauss-Seidel <br> time marching scheme. |
| implicit.rk3.R.petsc | Krylov-based Implicit (Runge-Kutta R, 3rd order). |
| implicit.rk4.R.petsc | Krylov-based Implicit (Runge-Kutta R, 4th order). |
| implicit.b2.petsc | Krylov-based Implicit (B2). |

Table 8.86: Time marching methods

## Iterations

| Syntax | -iterations \# |
| :---: | :---: |
| Description | Set the number of iterations. For unsteady flows this would be the number of iterations of the whole simulation. For dual time this would be the maximum iterations of the current time step. |
| Parameters | \# Number of iterations. |
| Examples | -iterations 1000 |

Table 8.87: Solve iterations option

## Time.step.reduction

| Syntax | -time.step.reduction \#attempts |
| :--- | :--- |
| Description | Set time the number of consecutive CFL reduction attempts when <br> non-physical values are detected in the solution. |
| Parameters | \#attempts $\quad$ Number of attempts. |
| Examples | -time.step.reduction 3 |

Table 8.88: Solve time.step.reduction option

## Dual.time

Syntax $\quad$-dual.time \#steps \#time-step

Description Set dual time stepping simulation.

| Parameters | \#steps | Number of physical time steps. |
| :--- | :--- | :--- |
|  | \#time-step | Physical time step $(\Delta t)$. |
| Examples | -dual.time 200 0.0001 |  |

Table 8.89: Solve dual.time option

## Global.minimal.timestep

| Syntax | -global.minimal.timestep |
| :--- | :--- |
| Description | Forces all the cells to use the global minimal time step that was <br> calculated. |
| Parameters | N/A |
| Examples | -global.minimal.timestep |

Table 8.90: Solve global.minimal.timestep option

| Save |  |
| :--- | :--- |
| Syntax | -save \# |
| Description | Set the intermittency of output of restart files. |
| Parameters | $\#$ |$\quad$ Number of steps between output. | Examples | -save 10 |
| :--- | :--- |

Table 8.91: Solve save option

## Save.path

| Syntax | -save.path \$path |
| :--- | :--- |
| Description | Set the path for output of log and restart files. |
| Parameters | \$path $\quad$ Path of log and restart files. |
| Examples | -save.path ./save/ |

Table 8.92: Solve save.path option

## Save.sequential

| Syntax | -save.sequential |
| :--- | :--- |
| Description | Adds iteration signature to the saves. |
| Parameters | N/A |
| Examples | -save.sequential |

Table 8.93: Solve save.sequential option

## Load.path

| Syntax | -load.path \$path |
| :--- | :--- |
| Description | Set the path for restart files. |
| Parameters | \$path $\quad$ Path of restart files. |
| Examples | -load.path ./load/ |

Table 8.94: Solve load.path option

## Load.sequence

| Syntax | -load.sequence \#iteration |
| :--- | :--- |
| Description | Load a specific iteration. |
| Parameters | \#iteration $\quad$ Iteration for load. |
| Examples | -load.sequence 1000 |

Table 8.95: Solve load.sequence option

## EOS

Syntax -eos \$eos

Description Set the equation of state.

| Parameters | \$eos | Equation of state. Currently, only perfect <br> gases are supported. |
| :--- | :--- | :--- |
| Examples | -eos air |  |

Table 8.96: Solve eos option

## Molecular

| Syntax | -molecular \$molecular |
| :--- | :--- |
| Description | Set the name of the molecular viscosity and thermal conductivity <br> to use. |
| Parameters | \$molecular $\quad$ Molecular relations name. |
| Examples | -molecular air-suther |

Table 8.97: Solve molecular option

| $\mathbf{P}$ |  |
| :--- | :--- |
| Syntax | $-\mathrm{p} \#$ |
| Description | Set the free stream pressure. |
| Parameters | $\#$ |
| Examples | -p 101325 |

Table 8.98: Solve p option

| T |  |
| :--- | :--- |
| Syntax | $-\mathrm{T} \#$ |
| Description | Set the free stream temperature. |
| Parameters | $\#$ |$\quad$ Free stream temperature. |  |
| :--- |
| Examples |

Table 8.99: Solve T option

## Mach

Syntax -Mach \#

Description Set the free stream Mach number.

| Parameters | $\#$ | Free stream Mach number. |
| :--- | :--- | :--- |
| Examples | - Mach 0.8 |  |

Table 8.100: Solve Mach option

## Velocity.magnitude

| Syntax | -velocity.magnitude $\#$ |
| :--- | :--- |
| Description | Set the free stream velocity magnitude. |
| Parameters | $\#$ |
| Examples | -velocity.magnitude 200 |

Table 8.101: Solve velocity magnitude option

## U

| Syntax | $-\mathrm{u} \#$ |
| :--- | :--- |
| Description | Set the free stream $X$ coordinate direction velocity component. |
| Parameters | $\#$ | | Free stream $X$ coordinate direction velocity |
| :--- |
| component. |

Examples -u 200

Table 8.102: Solve u option

| $\mathbf{V}$ |  |  |
| :--- | :--- | :--- |
| Syntax | $-\mathrm{v} \#$ |  |
| Description | Set the free stream $Y$ coordinate direction velocity component. |  |
| Parameters | $\#$ | Free stream $Y$ <br> component. |
| Examples | -v 0 |  |

Table 8.103: Solve v option

| $\mathbf{W}$ |  |
| :--- | :--- |
| Syntax | $-\mathrm{w} \#$ |
| Description | Set the free stream $Z$ coordinate direction velocity component. |
| Parameters | $\#$ |
| Free stream $Z$ coordinate direction velocity <br> component. |  |
| Examples | -w 20 |

Table 8.104: Solve w option

## Alpha

| Syntax | -alpha $\#$ |  |
| :--- | :--- | :--- |
| Description | Set the free stream angle of attack. |  |
| Parameters | $\#$ | Free stream angle of attack in degrees. |
| Examples | -alpha 10 |  |

Table 8.105: Solve alpha option

## Beta

| Syntax | -beta \# |  |
| :--- | :--- | :--- |
| Description | Set the free stream side slip angle. |  |
| Parameters | $\#$ | Free stream side slip angle in degrees. |
| Examples | -beta 0 |  |

Table 8.106: Solve beta option

## Trb.intensity

| Syntax | -trb.intensity \# |  |
| :--- | :--- | :--- |
| Description | Set the free stream turbulence intensity. |  |
| Parameters | $\#$ | Free stream turbulence intensity (in absolute <br> fraction, not percentage). |
| Examples | -trb.intensity 0.01 |  |

Table 8.107: Solve trb.intensity option

## Trb.mt

| Syntax | -trb.mt \#mt |  |
| :--- | :--- | :--- |
| Description | Set the free stream turbulence viscosity. |  |
| Parameters | $\# \mathrm{mt}$ | Free stream turbulence viscosity (in absolute <br> fraction from the molecular viscosity, not per- <br> centage). |
| Examples | -trb.mt 0.01 |  |

Table 8.108: Solve trb.mt option

## Reference.mach.trb

| Syntax | -reference.mach.trb \#ref |
| :--- | :--- |
| Description | Set the reference Mach number for the turbulence model (used to <br> override the freestream Mach number). |
| Parameters | \#ref $\quad$ Freestream Mach number. |
| Examples | -reference.mach.trb 0.7 |

Table 8.109: Solve reference.mach.trb option

## Reference.velocity.trb

| Syntax | -reference.velocity.trb \#ref |
| :--- | :--- |
| Description | Set the reference velocity for the turbulence model (used to override <br> the freestream velocity). |
| Parameters | $\#$ ref $\quad$ Freestream velocity $[\mathrm{m} / \mathrm{s}]$. |
| Examples | -reference.velocity.trb 210 |

Table 8.110: Solve reference.velocity.trb option

## Reference.mach

| Syntax | -reference.mach \#ref |
| :--- | :--- |
| Description | Set the reference Mach number. Default is the mean flow free <br> stream Mach number. |
| Parameters | \#ref $\quad$ Reference Mach number. |
| Examples | -reference.mach 0.75 |

Table 8.111: Solve reference.mach option

## Reference.velocity

| Syntax | -reference.velocity \#ref |
| :--- | :--- |
| Description | Set the reference velocity. Default is the mean flow free stream <br> velocity. |
| Parameters | \#ref $\quad$ Reference velocity. |
| Examples | -reference.velocity 300 |

Table 8.112: Solve reference.velocity option

## Reference.longitudinal

| Syntax | -reference.longitudinal \#ref |
| :--- | :--- |
| Description | Set the reference length for Reynolds number evaluation. Unused <br> by the current version. |
| Parameters | \#ref $\quad$ Reference length. |
| Examples | -reference.length 1.5 |

Table 8.113: Solve reference.length option

## Ref

| Syntax | -ref. $\$ \#\{\# \#\}$ |
| :--- | :--- |
| Description | Set the reference length, area, and reference point for force and <br> moment coefficient calculations. |
| Parameters | -reference.area $\quad$ Reference area (scalar). |
|  | -reference.point $\quad$Reference point (vector). |
|  | \# Reference value. |

Table 8.114: Solve ref option

## Plot

| Syntax | -plot [plot-options] ... |
| :--- | :--- |
| Description | Add to the fvuns file. See Table 8.116 for plot options list. |
| Parameters | N/A |
| Examples | -plot rank owner orig |

Table 8.115: Solve plot option

## Solve Plot Options

| Log type | Description |
| :--- | :--- |
| rank | Add the rank to the fvuns plot file. |
| part | Add the part to the fvuns plot file. |
| owner | Add ownership to the fvuns plot file. |
| orig | Add original node index to the fvuns plot file. |

Table 8.116: Solve plot options

## Log

| Syntax | $-\log \$ \log [\log$-options $] \ldots$ |
| :--- | :--- |
| Description | Report in log file. See Table 8.118 for log options list. |
| Parameters | $\$ \log \quad$ Log name. |
| Examples | -log progress-logs iter step time |

Table 8.117: Solve log option

## Solve Log Options

| Log type | Description |
| :--- | :--- |
| iter | Iteration number. |
| step | Step number. |
| pos | Position \# (iteration for steady state, step for dual time <br> simulation). <br> time |
| exec.time | Physical time for dual time simulation. |
| iter.avg.time | iteration average time. |
| iteration.time | Iteration time. |
| step.time | Step time. |
| petsc.mem.usage | Petsc memory usage in mebibyte. |
| petsc.mem.malloc | Petsc memory malloc in mebibyte. |

Table 8.118: Solve log options

## Wall.distance

| Syntax | -wall.distance $\{$ exact $[\# \mathrm{fx} \# \mathrm{fy} \# \mathrm{fz} \# \mathrm{cx} \# \mathrm{cy} \# \mathrm{cz}]\} \mid\{q u i c k[\# \mathrm{fx}$ \#fy \#fz]\} |
| :---: | :---: |
| Description | Set the wall distance algorithm, $\mathrm{fx}, \mathrm{fy}$, fz determine the boundary division allocation (surface) while cx, cy, cz determine the cell division allocation (volume). |
| Parameters | exact Exact wall distance calculation. |
|  | quick Use the quick algorithm. |
|  | $\# \mathrm{fx} \# \mathrm{fy} \# \mathrm{fz} \quad$ Number of division of surface faces in $\mathrm{x}, \mathrm{y}$, and, z directions. |
|  | \#cx \#cy \#cz Number of division of volume cells in $\mathrm{x}, \mathrm{y}$, and, z directions. |
| Examples | -wall.distance exact |

Table 8.119: Solve wall distance option

### 8.13 PETSc Toolkit

PETSc, the Portable, Extensible Toolkit for Scientific Computation is a suite of data structures and routines for the scalable (parallel) solution of scientific applications modeled by partial differential equations. PETSc is developed as open-source.

The PETSc input option section starts with the --petsc directive, followed by a series of petsc options. For advanced usage of the PETSc package the user is referred to the command line help or the online PETSc manual.

### 8.14 UNS Options

The UNS input options section start with the --uns directive, followed by a series of uns options.

Name

| Syntax | -name \$name |  |
| :--- | :--- | :--- |
| Description | Name of flow case. |  |
| Parameters | \$name $\quad$ Flow case name. |  |
| Examples | -name naca0012_laminar |  |

Table 8.120: UNS name option

## Prefix

| Syntax | \{-prefix $\mid$-prefix.starcd $\mid$-prefix.cgns \} \$prefix |  |
| :--- | :--- | :--- |
| Description | Set prefix of the flow case. |  |
|  | prefix | Used for manual conversion (conversion and <br> decomposition has been conducted using <br> star2metis or cgns2metis). |
| Parameters | prefix.starcd | Use original Star-CD export grid files (conver- <br> sion and decomposition is conducted). |
|  | prefix.cgns | Use original CGNS export grid files (conver- <br> sion and decomposition is conducted). |
| Eprefix | Prefix of flow case. |  |

Table 8.121: UNS prefix option

Key

| Syntax | -key \$prefix |
| :--- | :--- |
| Description | Save/load a key file. The file contains pre-calculated wall distance. <br> If the file exists, the code reads it prior to execution. If the file does <br> not exist, the code generates one. |
| Parameters | \$prefix $\quad$ Prefix of the key file. |
| Examples | -key ./NACA0012-Str-Laminar-Rey500 |

Table 8.122: UNS key option

## Scale

Syntax $\quad-$ scale \#x \#y \#z

Description Scale the grid.

|  | $\# \mathrm{x}$ | Scale in the $x$ direction. |
| :--- | :--- | :--- |
| Parameters | $\# \mathrm{y}$ | Scale in the $y$ direction. |
|  | $\# \mathrm{z}$ | Scale in the $z$ direction. |
| Examples | - scale 0.0010 .001 | 0.001 |

Table 8.123: UNS scale option

| Log |  |
| :--- | :--- |
| Syntax | $-\log \$ \log [$ log-options] ... |
| Description | Report in log file. See Tables 8.125 and |
| 8.133 for log options list. |  |
| Parameters | $\$ \log$ |
| Lxamples | $-\log$ coefficients cl cd |

Table 8.124: UNS log option

## UNS Log Options

| Log type | Description |
| :---: | :---: |
| wet.surface | Wet surface area. |
| p.center.x | Center of pressure $x$ coordinate. |
| p.center.y | Center of pressure $x$ coordinate. |
| p.center.z | Center of pressure $x$ coordinate |
| p.center.xFy | Center of pressure $x$ coordinate. |
| p.center.xFz | Center of pressure $x$ coordinate. |
| p.center.yFx | Pressure center sum $(\mathrm{y}$ * dFx) / Fx coordinate. |
| p.center.yFz | Pressure center sum $(\mathrm{y}$ * dFz) / Fz coordinate. |
| p.center.zFx | Pressure center sum(z * dFx) / Fx coordinate. |
| p.center.zFy | Pressure center sum $\mathrm{z}^{*} \mathrm{dFy}$ ) / Fy coordinate . |
| fx | $X$ coordinate direction force. |
| fy | $Y$ coordinate direction force. |
| fz | $Z$ coordinate direction force. |
| fx.pressure | Force in x direction due to pressure. |
| fy.pressure | Force in y direction due to pressure. |
| fz.pressure | Force in z direction due to pressure. |
| fx.friction | Force in x direction due to friction. |
| fy.friction | Force in y direction due to friction. |
| fz.friction | Force in z direction due to friction. |
| lift | Lift force. |
| drag | Drag force. |
| mx | Moment about $X$ coordinate direction. |

```
my Moment about }Y\mathrm{ coordinate direction.
mz Moment about Z coordinate direction.
cfx X coordinate direction force coefficient.
cfy Y coordinate direction force coefficient.
cfz Z coordinate direction force coefficient.
cmx Moment coefficient about X coordinate direction.
cmy Moment coefficient about Y coordinate direction.
cmz
cl
Lift coefficient.
cd
Drag coefficient.
```

Table 8.125: UNS log options

### 8.14.1 Motion: DOF Options

This section describes the directive to control motion. The current version of Arion supports a user prescribed motion only. The motion can be prescribed as a constant motion, a harmonic motion, or a motion prescribed using a discrete table. Table values can be loaded from a separate text file using a file directive. If a discrete table is utilized, the values of the table are interpolated as required.

## DOF Angular Motion

| Syntax | \{-dof.angular.roll.rate.motion \| -dof.angular.pitch.rate.motion | -dof.angular.yaw.rate.motion\} \{rad | deg\} \{\#rate [sin \#amplitude \#frequency \#shift] | table.t [\#t0 \#v0 \#t1 \#v1 ... \#tN \#vN | file \#filename ] table.end |
| :---: | :---: |
| Description | Set angular rate motion where rate $=\#$ rate $+\#$ amplitude ${ }^{*}$ $\cos \left(\#\right.$ frequency ${ }^{*} \mathrm{t}+\#$ shift $)$. |
| Parameters | $\operatorname{rad}$ Set rate in radians per second. |
|  | deg Set rate in degrees per second. |
|  | \#rate Angular rate. |
|  | \#amplitude Oscillation amplitude. |
|  | \#frequency $\quad$ Oscillation frequnecy. |
|  | \#shift Oscillation phase shift. |
|  | $\# \mathrm{t} 0 \# \mathrm{t} 1 . . . \# \mathrm{tN} \quad$ Discrete time. |
|  | $\# \mathrm{v} 0 \# \mathrm{v} 1 \ldots$.. $\mathrm{vN} \quad$ Discrete rate. |
| Examples | -dof.angular.roll.rate.motion deg 5 |

Table 8.126: UNS DOF angular rate motion option

## DOF Velocity Motion

| Syntax | -dof.velocity.motion $\{\# \mathrm{u} \# \mathrm{v} \# \mathrm{w} \mid$ table.t $[\# \mathrm{t} 0 \# \mathrm{u} 0 \# \mathrm{v} 0 \# \mathrm{w} 0 \# \mathrm{t} 1$ \#u1 \#v1 \#w1 ... \#tN \#uN \#vN \#wN \| file \#filename ] table.end $\}$ |  |
| :---: | :---: | :---: |
| Description | Set motion velocity components. |  |
| Parameters | \#u | $X$ coordinate dire |
|  | \#v | $Y$ coordinate direc |
|  | \#w | $Z$ coordinate direc |
|  | \#t0 \#t1 ... \#tN | Discrete time. |
|  | $\# \mathrm{u} 0 \# \mathrm{u} 1 \ldots$.. uN | Discrete velocity. |
|  | $\# \mathrm{v} 0 \# \mathrm{v} 1 \ldots \# \mathrm{vN}$ | Discrete velocity. |
|  | \#w0 \#w1 ... \#wN | Discrete velocity. |
| Examples | -dof.velocity.motion 10000 |  |

Table 8.127: UNS DOF velocity motion option

## DOF Acceleration Motion



Table 8.128: UNS DOF acceleration motion option

## DOF Angular Init

| Syntax | \{-dof.angular.roll.rate.init $\|$dof.angular.pitch.rate.init <br> -dof.angular.yaw.rate.init $\}\{\operatorname{rad} \mid \operatorname{deg}\}$ \#rate <br> Description | Set initial value of angular rate. |
| :--- | :--- | :--- |
|  | rad | Set rate in radians per second. |
| Parameters | deg | Set rate in degrees per second. |
|  | \#rate | Angular rate. |
| Examples | -dof.angular.roll.rate.init deg 5 |  |

Table 8.129: UNS DOF angular rate init option

## DOF Velocity Init

| Syntax | -dof.velocity.init $\# \mathrm{u} \mathrm{\# v} \# \mathrm{w}$ |  |
| :--- | :--- | :--- |
| Description | Set initial velocity components. |  |
|  | $\# \mathrm{u}$ | $X$ coordinate direction velocity component. |
| Parameters | $\# \mathrm{v}$ | $Y$ coordinate direction velocity component. |
|  | $\# \mathrm{w}$ | $Z$ coordinate direction velocity component. |
| Examples | - dof.velocity.init 100200 |  |

Table 8.130: UNS DOF velocity init option

## DOF Acceleration Init

| Syntax | -dof.acceleration.init \#u \#v \#w |  |
| :--- | :--- | :--- |
| Description | Set initial acceleration components. |  |
|  | \#ax | $X$ coordinate direction acceleration component. |
| Parameters | \#ay | $Y$ coordinate direction acceleration component. |
|  | \#az | $Z$ coordinate direction acceleration component. |
| Examples | -dof.acceleration.init 100200 |  |

Table 8.131: UNS DOF acceleration init option

## DOF Motion Origin

| Syntax | -dof.origin.of.motion $\# \mathrm{x} \# \mathrm{y} \# \mathrm{z}$ |  |
| :--- | :--- | :--- |
| Description | Set the origin of motion. |  |
|  | $\# \mathrm{x}$ | $X$ coordinate direction component. |
| Parameters | $\# \mathrm{y}$ | $Y$ coordinate direction component. |
|  | $\# \mathrm{z}$ | $Z$ coordinate direction component. |
| Examples | -dof.origin.of.motion 000 |  |

Table 8.132: UNS DOF motion origin option

## DOF Log Options

| Log type | Description |
| :---: | :---: |
| dof.phi | Phi-euler angle in body frame. |
| dof.theta | Theta - euler angle in body frame. |
| dof.psi | Psi - euler angle in body frame. |
| dof.p | p - angular velocity in body frame. |
| dof.q | q - angular velocity in body frame. |
| dof.r | r - angular velocity in body frame. |
| dof.p.dot | $\mathrm{dp} / \mathrm{dt}$ - angular acceleration in body frame. |
| dof.q.dot | dq/dt - angular acceleration in body frame. |
| dof.r.dot | $\mathrm{dr} / \mathrm{dt}$ - angular acceleration in body frame. |
| dof.all.angular | All angualr information. |
| dof.dx | x - translational offset in observer frame. |
| dof.dy | y - translational offset in observer frame. |
| dof.dz | z - translational offset in observer frame. |
| dof.u | $u$ - translational velocity in observer frame. |
| dof.v | v - translational velocity in observer frame. |
| dof.w | w-translational velocity in observer frame. |
| dof.u.dot | $\mathrm{du} / \mathrm{dt}$ - translational acceleration in observer frame. |
| dof.v.dot | $\mathrm{dv} / \mathrm{dt}$ - translational acceleration in observer frame. |
| dof.w.dot | $\mathrm{dw} / \mathrm{dt}$ - translational acceleration in observer frame. |
| dof.all.translational | All translational information. |
| dof.origin.of.motion | Origin of motion vector. |
| dof.origin.of.motion.x | Origin of motion x - coordinate. |


| dof.origin.of.motion.y | Origin of motion y - coordinate. |
| :--- | :--- |
| dof.origin.of.motion.z | Origin of motion z - coordinate. |

Table 8.133: DOF log options

### 8.15 Run-time Options

Arion provides the capability to control the run while the application is running using the run-time options. This can be achieved by creating an ascii text file named 'arion.ins' containing one of the following run-time options:

## Run-time Options

| Option | Action |
| :--- | :--- |
| stop | Stop and save a restart. |
| kill | Immediately stop the run (even in dual-time mode) <br> and save a restart. |
| save | Dump the FVUNS file as requested by the user at the <br> next available opportunity. |
| time.step [\$system] \#cfl | Save a restart. <br> Change to the specified constant CFL or virtual time <br> step of all the systems or the specified \$system. |
| dt \#dt | Change to the specified physical time step (for dual <br> time simulations). |

Table 8.134: Run-time options

### 8.15.1 Run-time Options Examples

The examples in Table 8.135 provide the complete Unix/Linux command to create the 'arion.ins' file with the required content. Alternatively, the user may use an editor to create the file and enter the content. Note, once Arion identifies the existence of the file 'arion.ins' and reads its content, the file is erased.

## Run-time Options Examples

| Command | Result |
| :--- | :--- |
| echo stop $>$ arion.ins | Stop and save a restart. |
| echo plot $>$ arion.ins | Dump the FVUNS file as requested by the user <br> at the next available opportunity. |
| echo save $>$ arion.ins | Save a restart. |
| echo time.step 50.0 > arion.ins | Change the CFL or time step to 50.0 (all sys- <br> tems). |
| echo time.step turbulent.kw.tnt | Change the CFL or virtual time step for the <br> k- $\omega$-TNT turbulence model equations to 30.0. |
| $30.0>$ arion.ins | Change the physical time step to 0.001 |
| echo dt 0.001 |  |

Table 8.135: Run-time options examples

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[^0]:    ${ }^{1}$ Equation (4.3) without the index

